



# THE STUDY OF I-Q SIGNAL GENERATION USING COMPLEX FILTER BASED $\Delta\Sigma$ D/A MODULATOR FOR COMMUNICATION APPLICATION

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## ABSTRACT

This paper describes the study of application of a complex bandpass  $\Delta\Sigma$  D/A modulator as Quadrature (I-Q) signal generation in communication system for communication Integrated Circuit (IC) testing as well as transmitter. The study shows that the complex bandpass  $\Delta\Sigma$  D/A modulator is superior compared to two real-bandpass  $\Delta\Sigma$  D/A modulators regarding to noise-shaping characteristics. Hence, the trade-off between bandwidth and sampling speed is better for the complex bandpass  $\Delta\Sigma$  D/A modulator. This study also presents the theoretical analysis and simulation results of its extension and complex multi-bandpass modulator characteristics. From the result,

**Keywords:** complex filter, complex bandpass, multi-band, D/A modulator.

## INTRODUCTION

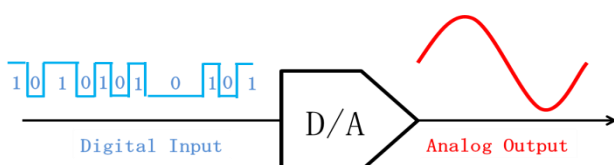
Demands for low cost, low power and high performance of a digital-to-analog (D/A) (Figure-1) converter are significantly increased especially in communication applications. Since communication devices become inexpensive and more sophisticated, the D/A converter circuits in their transmitter parts (which often generate I-Q signals) become more complicated and challenging. Nevertheless, the Very Large Scale Integration (VLSI) fabrication cost reduces with the advancement of VLSI process technology. The successful market of the portable devices is also a factor that contributes to the high demands of low cost and high performance of D/A converter. Most of these devices also require for a low power D/A converter to allow them operate at operating voltage which mostly uses battery.

On the other hand, the testing cost of a IC device increases due to the circuit complexity and high specification requirements. The testing of the communication ICs requires high quality I-Q signal at low cost, and in many cases, D/A converters used to produce I-Q signal generation (Vasan *et al.*, 2012), (Abe *et al.*, 2014), (Byoungcho and Abraham, 2014), (Khafaji *et al.*, 2014).

This paper discusses applicability of a complex bandpass  $\Delta\Sigma$  D/A modulator to generate I-Q signals rich configuration.

## D/A CONVERTER FOR I-Q SIGNAL GENERATION

This section discusses advantages and drawbacks of the existing architectures for I-Q signal generation. The architectures can be classified as follow:



**Figure-1.** D/A converter with its input and output signals.

1) Analog method.  
2) Digital method (DSP + D/A converters, or Direct Digital Synthesizer).

2-1) DSP + two Nyquist-rate D/A converters + two analog filters.

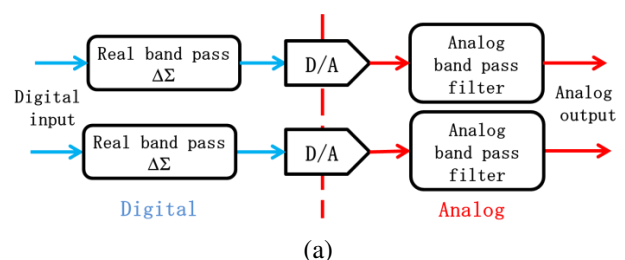
2-2) DSP + two real-bandpass  $\Delta\Sigma$  D/A converters + two analog filters.

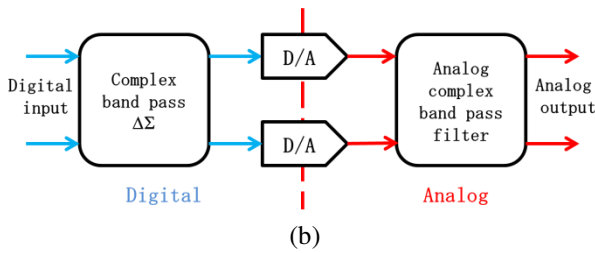
2-3) DSP + one complex-bandpass  $\Delta\Sigma$  D/A converter + one analog complex filter.

As the VLSI technology progresses, digital method becomes much easier to design. The method 2-1) requires relatively large Nyquist-rate D/A converters and analog filters. The method 2-2) uses two digital  $\Delta\Sigma$  modulators (whose circuits are negligible in fine Complementary Metal Oxide Semiconductor Large Scale Integration (CMOS LSI)) and two 1-bit D/A converters (which are also negligible), and also requirements for two analog filters can be relaxed due to the oversampling. The same arguments hold for the method 2-3) as those of the method 2-2).

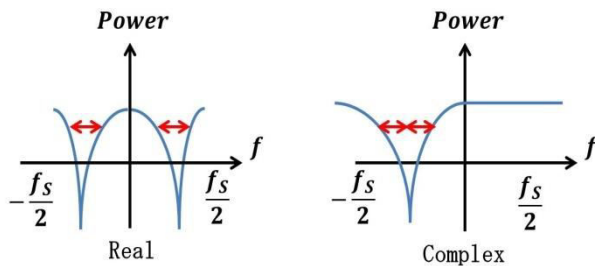
Figure-2 shows block diagrams for the methods 2-2) and 2-3). Up-conversion mixers with local oscillators may follow the analog filters in the digital methods (Otsuki *et al.*, 2005).

## COMPLEX BANDPASS $\Delta\Sigma$ D/A MODULATOR FOR I-Q SIGNAL GENERATION





**Figure-2.** I-Q signal generation with  $\Delta\Sigma$ D/A modulation. (a) Two real-bandpass modulators (method (2-2)) and (b) One complex bandpass modulator (method (2-3)).



**Figure-3.** Noise-shaping characteristics. (Left) Real bandpass modulator. (Right) Complex bandpass modulator.

Now let us compare the methods 2-2) and 2-3). Suppose that the centre of the I-Q signal band is  $-f_s/4$ . Then as Figure-3 shows, the noise-shaping characteristics for the complex modulator around  $-f_s/4$  is better than that of the real bandpass modulators (in other words, the quantization noise in the signal band is lower in complex modulator case).

The complexity of two real analog filters and one analog complex filter would be comparable. Hence, the method 2-3) (which uses complex signal processing) would be better than the method 2-2).

Remark: One might argue that better noise-shaping characteristics can obtain higher-order real bandpass modulators and digital modulators are free in fine CMOS LSI. However, higher-order modulators require higher-order analog filters following the modulators, and hence comparison of complex and real bandpass modulators with the same order would be fair.

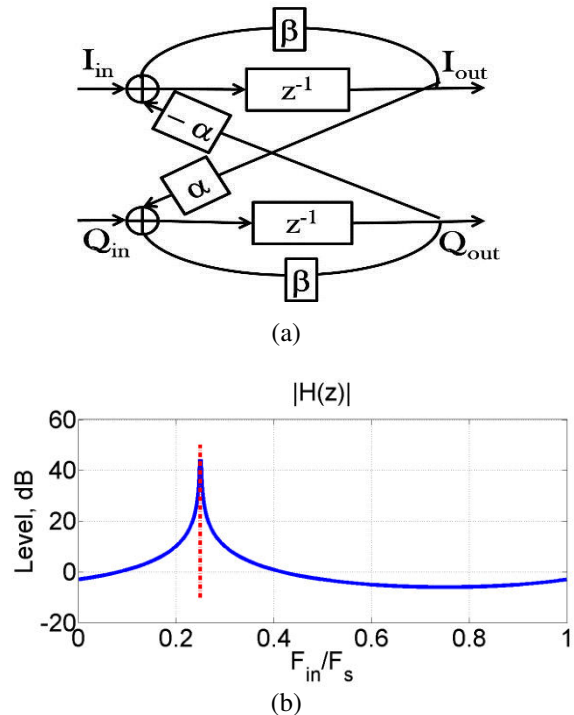
### COMPLEX BANDPASS $\Delta\Sigma$ D/A MODULATOR

This section describes the complex bandpass  $\Delta\Sigma$ D/A modulator in details. Figure-2 and Figure-3 show the illustration of advantages of a complex bandpass  $\Delta\Sigma$ D/A modulator compared to two real bandpass  $\Delta\Sigma$ D/A modulators. By using this type of modulator, larger bandwidth (or better Signal-to-Noise Ratio (SNR)) can be obtained due to its asymmetric behaviour with respect to  $\omega_s = 0$ . In contrast, the real bandpass modulator has a symmetric behaviour with respect to  $\omega_s = 0$  with 2 poles at two different points and it provides only a half bandwidth for each pole (Otsuki *et al.*, 2005),

(Shreier and Temes, 2005), (San *et al.*, 2007), (Martins, 2004), (Kobayashi *et al.*, 2002).

### Complex bandpass filter

Figure-4(a) shows the structure of a basic complex filter.



**Figure-4.** (a) Complex filter and (b) its gain characteristics.

From Figure-4(a), the gain of the system can be determined by obtaining their transfer function (Figure-4(b)). First, the equations derived from inputs to outputs as follows:

$$I_{out}(z) = I_{in}z^{-1} - \alpha Q_{out}z^{-1} + \beta I_{out}z^{-1} \quad (1)$$

$$Q_{out}(z) = Q_{in}z^{-1} + \alpha I_{out}z^{-1} + \beta Q_{out}z^{-1} \quad (2)$$

Next, complex input  $V_{in}(n)$  and complex output  $V_{out}(n)$  as follows:

$$V_{in}(z) = I_{in}(z) + jQ_{in}(z) \quad (3)$$

$$V_{out}(z) = I_{out}(z) + jQ_{out}(z) \quad (4)$$

Then, its transfer function,  $H(z)$  is defined as follows:

$$H(z) = \frac{V_{out}(z)}{V_{in}(z)} \quad (5)$$

Finally, the transfer function obtains as:

$$H(z) = \frac{1}{z - (\beta + j\alpha)} \quad (6)$$



### Complex bandpass $\Delta\Sigma$ D/A modulator

Figure-5(a) and Figure-6(a) show first-order and second-order complex bandpass  $\Delta\Sigma$  D/A modulators with the centre frequency  $-f_s/4$  of the signal band. Figure-5(b) and Figure-6(b) show their output spectrum for the complex sinusoidal signal input around  $-f_s/4$ , and it is shown that the quantization noise is shaped at  $-f_s/4$ . Here, value of  $\alpha=1$ ,  $\beta=0$  is used.

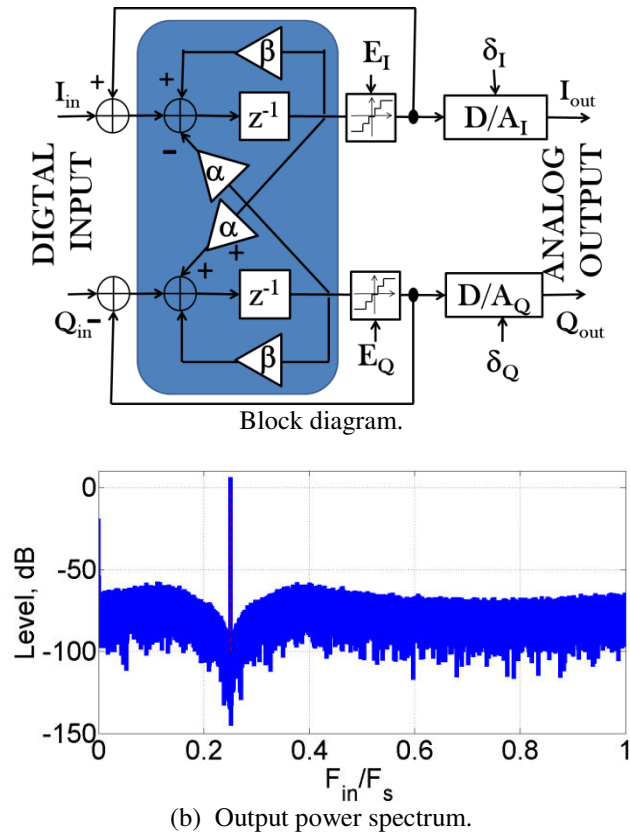


Figure-5. First-order complex bandpass  $\Delta\Sigma$  D/A modulator.

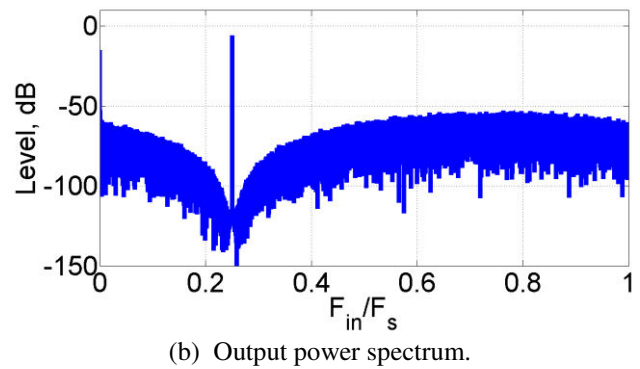
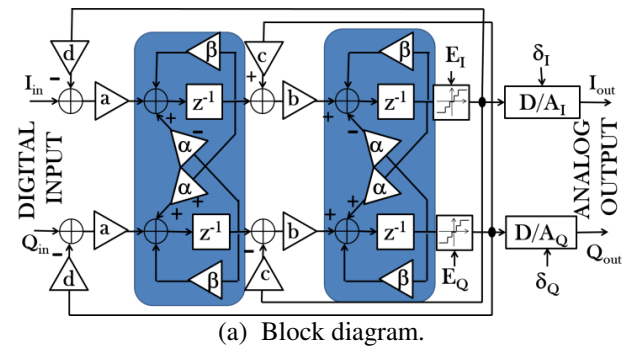


Figure-6. Second-order complex bandpass  $\Delta\Sigma$  D/A modulator.

### COMPLEX MULTI-BANDPASS $\Delta\Sigma$ D/A MODULATOR

This section describes complex multi-bandpass  $\Delta\Sigma$  D/A modulators for multi-tone I-Q signal generation (Motozawa *et al.*, 2007).

#### Complex multi-bandpass filter

Figure-7 shows a first-order complex multi-bandpass filter, and Figure-8 shows its gain characteristics for (a)  $n=2$  and (b)  $n=4$ .

Its transfer function given as follows:

$$H(z) = \frac{1}{z^n - (\beta + j\alpha)} \quad (7)$$

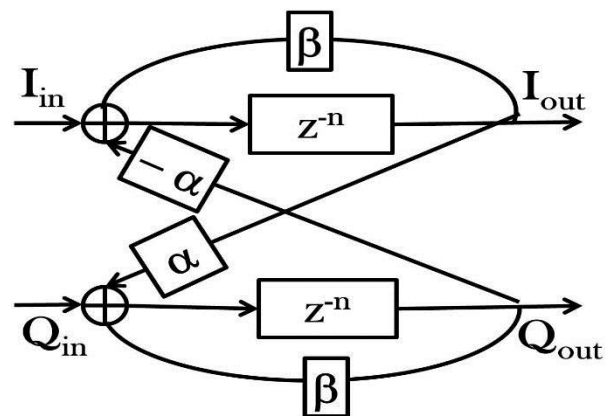
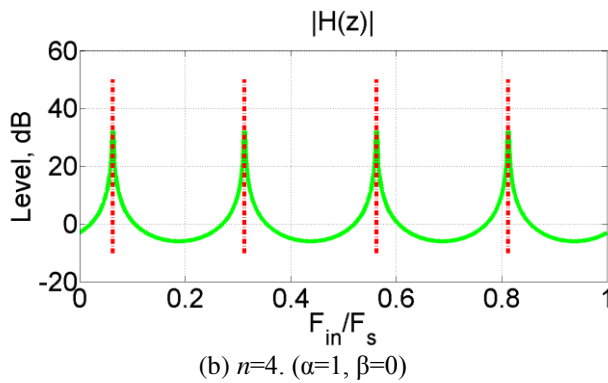
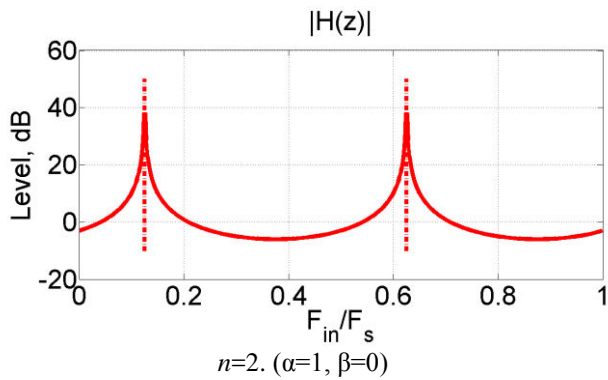


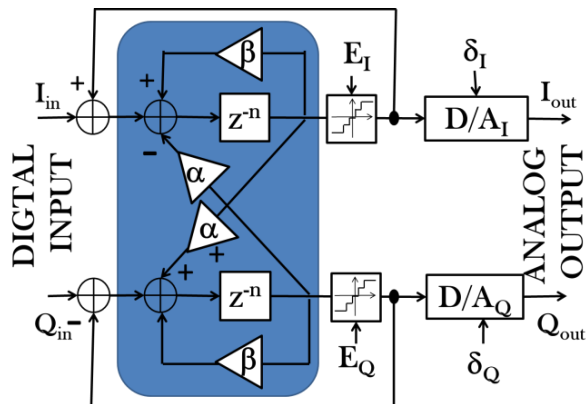
Figure-7. Complex multi-bandpass filter.



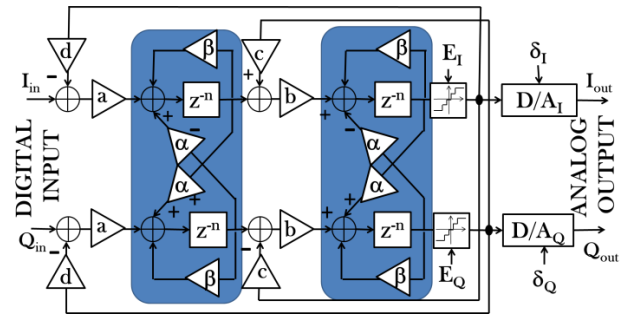
**Figure-8.** Gain characteristics of multi-band complex filters.

#### Complex multi-bandpass $\Delta\Sigma$ /A modulator

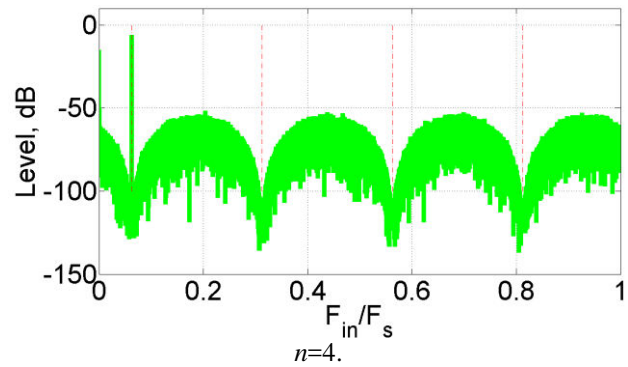
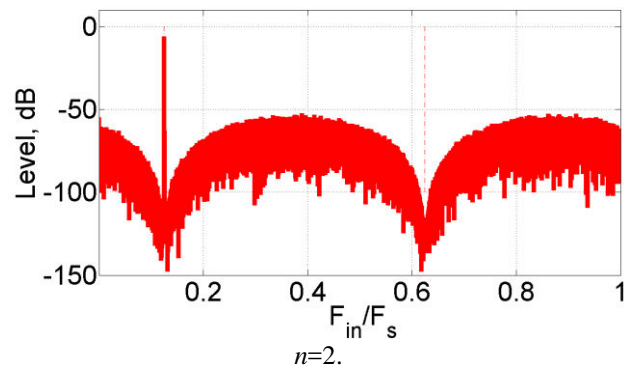
Figure-9 and Figure-10 show first-order and second-order complex multi-bandpass  $\Delta\Sigma$ /A modulators, and Figure-11 shows the simulated output power spectrum for the second-order with (a)  $n = 2$  and (b)  $n = 4$ . Figure-12 shows SNR versus OSR (oversampling ratio).



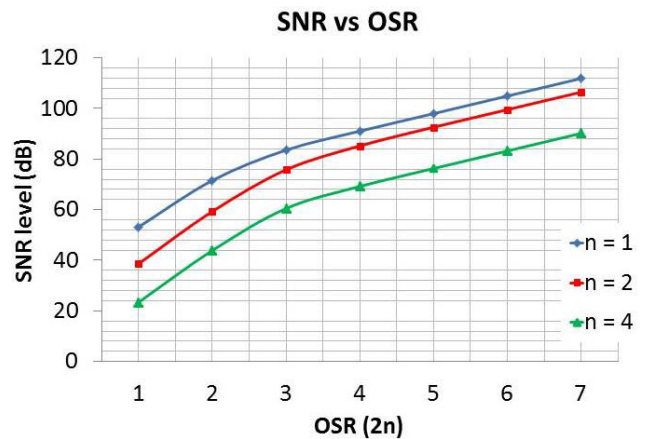
**Figure-9.** First-order complex multi-bandpass  $\Delta\Sigma$ /A modulator.



**Figure-10.** Second-order complex multi-bandpass  $\Delta\Sigma$ /A modulator.



**Figure-11.** Second-order complex multi-bandpass  $\Delta\Sigma$ /A modulator output spectrum.



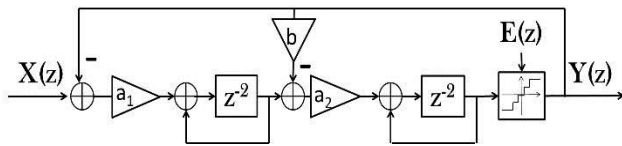
**Figure-12.** Simulated SNR versus OSR for second-order complex multi-bandpass  $\Delta\Sigma$ /A modulators.





## SIMULATION RESULT

The performance of complex compared to real bandpass modulator is verified using MATLAB simulator. For comparison study, a second-order complex modulator in Figure-6, and a second-order real bandpass modulator in Figure-13 is simulated. The simulation results show their noise-shaping behaviours in Figure-14(a) and Figure-14(b) for both real and complex bandpass respectively, and their OSR versus SNR performance as shown in Figure-15. As a result, the second-order complex modulator has better SNR by 10dB compared to the second-order real bandpass modulator.



**Figure-13.** A second-order real bandpass  $\Delta\Sigma D/A$  modulator used for simulation.

By set the value of  $a_1$ ,  $a_2$  and  $b$  as follow:

$$a_1 = 1, \quad a_2 = 1, \quad b = 2$$

The Signal Transfer Function (STF),  $STF(z)$  is defined as:

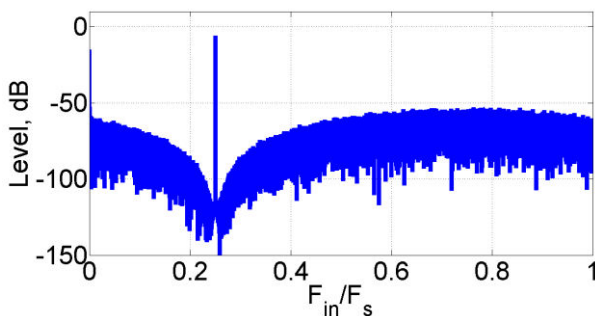
$$STF(z) = \frac{a_1 a_2 z^{-2}}{D(z)} \quad (8)$$

Then, the Noise Transfer Function (NTF),  $NTF(z)$  is defined as:

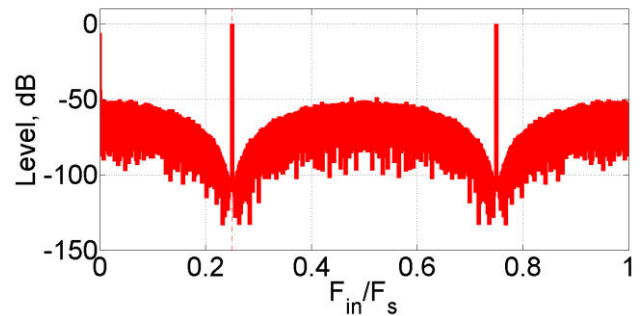
$$NTF(z) = \frac{(1-z^{-1})^2}{D(z)} \quad (9)$$

Finally, the denominator,  $D(z)$  can be expressed as:

$$D(z) = (1 - z^{-1})^2 + a_1 b z^{-1} (1 - z^{-1}) + a_1 a_2 z^{-2} \quad (10)$$

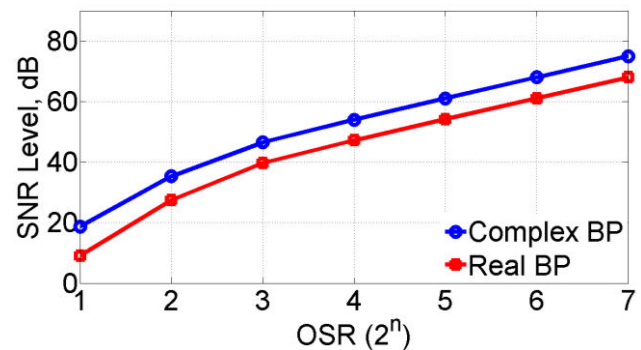


(a) The second-order complex bandpass modulator.



(b) The second-order real bandpass modulator.

**Figure-14.** Output spectrum comparison.



**Figure-15.** SNR versus OSR comparison between second-order complex and real bandpass  $\Delta\Sigma D/A$  modulators.

## CONCLUSIONS

From this study, it is found that:

- A first-order complex bandpass  $\Delta\Sigma D/A$  modulator has one pole between  $-f_s/2$  to  $f_s/2$ .
- A first-order real bandpass  $\Delta\Sigma D/A$  modulator has two poles between  $-f_s/2$  to  $f_s/2$ .
- A first-order complex multi-bandpass  $\Delta\Sigma D/A$  modulator has  $n$  poles between  $-f_s/2$  to  $f_s/2$ .

From the simulation results, it shows that a complex bandpass  $\Delta\Sigma D/A$  modulators has better performance in terms of in-band noise and wide bandwidth compared to real bandpass ones. Thus, it proves that a complex bandpass  $\Delta\Sigma D/A$  modulators would be a more suitable architecture for I-Q signal generation, while multi-bandpass is suitable for multi-tone I-Q signal generation.

Then for a given OSR, complex bandpass has the best SNR, followed by the real bandpass and lastly,  $n$ -bandpass one ( $n > 2$ ). Clarification of these relationships with analytical equations would be an interesting future work.

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