



OPTIMAL CODING PERFORMANCE FOR MIMO SYSTEM

K. Prabhakara Rao¹ and P. V. Sridevi²

¹Department of Electronics and Communication Engineering, B.V. Raju Institute of Technology, Narsapur, Telangana, India

²Department of Electronics and Communication Engineering, A.U. College of Engineering, Visakhapatnam, Andhrapradesh, India

E-Mail: prabhakar.kapula@gmail.com

ABSTRACT

Estimation of the channel and its performance under dynamic conditions have always remained a challenge for wireless communication domain. New techniques were developed for channel diversity and spectrum utilization. In this paper a new interference management with resource control is proposed, to achieve the objective of higher performance in MIMO systems, using interference conditions. A generic approach for both coordinated and randomized multi-user access strategies for interference mitigation is investigated. The suggested analytical framework develops the correlation of fading channel over the space-frequency domain and non-stationary features of the multipath interference to allocate resources for minimizing interference.

Keywords: MIMO system, coding performance, resource diversity, error estimation.

1. INTRODUCTION

Wireless channels are getting diverse in nature. The uncertainty in channel conditions has degraded the estimation performance of conventional channel estimator logic and needs an updating. The feedback estimators are hence developed to achieve the estimation performance under variant channel condition. Among the various approaches of channel estimation logic, feedback based estimators are used as a feedback estimator, which works with the objective of channel tracking. The estimation process is governed by a state transition logic, where the process of estimation and updating is carried out to obtain a estimate. In the process of MIMO-OFDM channel estimation, the application of feedback filters is made for its simpler coding and estimation performance. However, with the increase in communication approaches and offered services, the conventional model of feedback filtration is needed to be improved. To derive better performance for such system, different methods were developed in recent past. In [1] frequency selective fading channel estimation is proposed. The issue of channel imperfection is analyzed. A novel method of pilot expansion is proposed to capture the multipath signal arise in the MIMO system. A Decision feedback filter is proposed for channel tracking in the communication system. The approach of flexible pilot flexible coding is being presented. A joint estimation of channel gain and phase noise in MIMO system is analyzed in [2]. A decision directed extended feedback filter for phase noise tracking is developed. The approach of extended feedback filter is observed to be more stable in tracking phase noise estimation. A similar approach of channel estimation in semi-blind approach is proposed in [3]. A recursive estimation updating in feedback based estimation logic using blocks for MIMO system is employed. A dynamic block processing expansion model is presented to channel estimation for fast fading channel. The issue of diversity in MIMO-OFDM system is being analyzed in recent time. In [4] to achieve a faster divergence solution, a channel estimation algorithm based on feedback filter is developed. A state transfer coefficient (STC) is derived

with a threshold correction logic for the time varying environment. Towards the issue of user mobility, in [5,6] new scheme of mobility concern in MIMO-OFDM system is suggested. An intelligence logic using fuzzification was developed for variant format of slow, fast and medium speed mobility. The feedback filter is designed to perform the channel estimation for the signal received under mobility condition. The operational efficiency of a channel estimator is dependent on the channel impulse response estimation in MIMO-OFDM system. In [7] a channel impulse response estimation based on the correlation of transmits or receive antennas. An approach of concatenated wiener filters for the optimization of channel estimation by optimizing the channel characteristic in time and frequency domain. In [8], to estimates channels in different high speed mobile environments, a wiener filter based approach with basis expansion model (BEM) is presented. The suggested approach provides a better estimation under time variant channel condition. Towards effective estimation, in [9] a novel a symmetric extension method was suggested for OFDM system to reduce the MSE, leakage power and noise of conventional DFT. The estimation of partial frequency response is symmetrically extended as well as reduced MSE and noise eliminated with the very small power loss. In [10] an SCM based blind channel estimation method for zero padding MIMO-OFDM systems have the distinctive features. The identifiability condition is very simple and is more relaxed than the irreducible or column reduced condition. It can apply to the more transmit antennae case under a certain condition. Through numerical simulation, it yields improved BER performance in the low-to-moderate SNR region. In [11] a first order approximation method as well as a second order approximation method for joint CFO and CIR estimated in OFDM systems. In first order approximation method provides an adaptive iteration algorithm with excellent estimation and tracking range compare to the conventional. The Second order approximation method will improve frequency tracking range and channel estimation compared to the first order method. In [12] a channel estimator computes the long-



term features through a subspace tracking algorithm by identifying the invariant (over multiple OFDM symbols) space-time modes of the channel. On the other side, the fast-varying fading amplitudes are possibly tracked by using LS techniques that exploit temporal correlation of the fading process. In particular, MIMO-OFDM with BICM and MIMO-turbo equalization has been selected as a benchmark for performance evaluation in terms of BER. In [13] a semi-blind timing synchronization and channel estimation scheme for OFDM systems was developed based on unit vectors. Semi blind approach having three stages, (i) coarse timing offset with maximum gain is obtained in multipath fading channels, (ii) a fine time adjustment algorithm to find an actual time position in channels, (iii) based on final timing estimation obtained the frequency domain in channel response. In this paper, we propose a new methodology to assess the performance of MIMO-OFDMA systems over space frequencies elective channels and non-stationary interference. The performance is evaluated in terms of average bit error probability at the output of the forward error correction (FEC) decoder. We concentrate on convolution coding for this is the mandatory FEC scheme for the majority of the commercial standards based on OFDM with BICM technology. Nevertheless, the analysis based on the union bound approach is general and can be extended to either convolution or block codes. To provide a brief insight in the proposed methodology, let us consider the transmission of a codeword over a set of parallel sub-channels i.e., the OFDM subcarriers.

2. MIMO SYSTEM

Future wireless systems demand for high data rate offering so as to achieve the demanded objective. In conventional systems the available approaches are limited by inter-symbol-interference (ISI) due to the frequency selectivity of the wireless channel. To achieve a high throughput communication with minimum interference OFDM systems was proposed. By sending information in parallel with larger symbol durations, OFDM systems avoid the ISI significantly. To achieve high data rate the OFDM systems are enhanced via the exploitation of the MIMO technique. MIMO offers additional parallel channels in spatial domain to boost the data rate. Hence, MIMO-OFDM is a promising combination for the high data requirement of future wireless systems. Multiple input multiple output (MIMO) antenna systems with orthogonal frequency division multiple access (OFDMA) is the most promising combination of technologies for high data-rate services in next generation wireless networks. Performance assessment of multi-cell systems based on these technologies is of crucial importance in the deployment of broadband wireless standards such as WiMAX and 3GPP LTE.

A. System outline

In MIMO-OFDMA systems, the side information can be the correlation due to the time evolution of the channel, the correlation between channel taps and OFDM subcarriers. Many studies exploited time

and frequency domain correlation to get the advantages of both domains. With MIMO, correlation from the spatial domain exists. Spatial correlation arises due to close antenna spacing's and poor scattering environments. Coherent demodulation of the transmitted symbols requires accurate channel estimation. MIMO-OFDM channel estimation can perform in frequency and/or time domains. In frequency domain, channels at each OFDM sub-carrier are estimated. In time domain estimation, the unknowns are the channel length, tap delays, and their corresponding coefficients. Channel estimation methods can be improved by using the side information. In every cell the base station (BS) is equipped with $N_R \geq 1$ antennas and each of the subscriber stations (SSs) has an antenna array of $N_T \geq 1$ elements. The transmission is organized according to the logical frame, with K adjacent sub-carriers observed over L consecutive OFDM symbols. Within each cell, multiple accesses are handled by dividing the logical frame into frequency-time units (data regions) of $K \times L$ subcarriers each. The BS can assign one or more data regions to each SS. The multi-user scheduling strategy provides the mapping rule from the logical frame onto the physical resource to form the time-frequency physical frame. Since some of the sub-carriers might remain unassigned, the traffic load $\eta \leq 1$ is introduced to denote the number of active sub-carriers out of the total number. Depending on the degree of cooperation among BSs and on the traffic load η , every data region can experience up to N_i interferes with constant power over the whole data region. Differently from coordinated approach, the interference randomization policy employs a cell-specific permutation of the sub-carriers over the OFDMA bandwidth before mapping the logical sub-carriers onto the physical resources, for the purpose of randomizing the interference within each data region. In this paper, we consider both the coordinated and the randomized scheduling policy for the uplink case. Notice that for the former policy the scheduler of each BS could dynamically optimize the assignment of a certain data region to minimize the cross interference. However, since the optimization of the scheduler is beyond the scope of this paper, the assignments of the data regions are here assumed to be random and independent from cell to cell as for a non-optimized scheduler.

B. Channel model

In frequency-selective multipath environment, the $NR \times NT$ channel response H_k on the i_{th} subcarrier can be modeled as the sum of W path contributions:

$$H_k = G_k \sum_{r=1}^W \sqrt{P_r} A_r \exp(-j2\pi \frac{k}{N}) \quad (1)$$

Where each path is characterized by mean power P_r , the $NR \times NT$ fading amplitudes. The complex term G_k denotes the frequency response of the cascade connection of the transmitter and receiver filters on the i_{th} sub-carrier. The fading amplitudes are assumed to be Rayleigh distributed and uncorrelated from path to path, according to the wide sense stationary uncorrelated scattering model:



$$R_{S,r} = R_{Tx,r} \otimes R_{Rx,r} \quad (2)$$

Accounts for the spatial correlation of the fading channel, denoting the Kronecker product and with R_{Tx} , and R_{Rx} , being the spatial covariance's among the transmitting and receiving antennas respectively. Following the same reasoning's, we consider two different models corresponding to different assumptions about the correlation (2) and geometry of the antenna arrays: a beamforming model is adopted for antenna arrays with closely spaced apart elements and a diversity model for array elements that are sufficiently far apart. In this section we define two specific scenarios for performance assessment. If interference is spatially correlated, the covariance matrix (1) is structured and thus the multi-antenna combiner can exploit this knowledge to mitigate the inter-cell interference by an appropriate beamforming strategy. Inter-cell interference filtering by beam forming is here paired with coordinate scheduling policy as in this case the spatial structure of the interference remains the same over the data region with many practical benefits (e.g., the interference covariance can be estimated with a high degree of accuracy). On the other hand, uncorrelated interference, as for the diversity model, is coupled with randomized scheduling policy to maximally exploit the space/time/interference diversity. Even if the noise power is changing sub-carrier-by-sub-carrier according to (2), the receiver could realistically estimate the average interference power within the data region \mathcal{K} , $\sigma^2 = \frac{1}{KZ} \sum_{k \in \mathcal{K}} \sigma_k^2$ which is the interference level used in soft decoding. Based on these considerations, we define the following two typical scenarios:

C. Coordinated interference scenario

In the coordinated strategy, the data regions in all cells are mapped over adjacent, or piecewise-adjacent, sub-carriers, which make the interference pattern to be constant over the whole data region and thus $Q_k = Q$, for $k \in \mathcal{K}$. The stationarity of the interference configuration allows for an accurate estimate of the impairment covariance Q which can be efficiently exploited for interference mitigation. The MIMO-OFDMA system provides two dimensions that can be employed for interference reduction: the frequency domain of the OFDM signaling and the spatial domain offered by the array processing. To enhance the interference rejection capability, we adopt a uniform linear antenna array (ULA) with closely spaced apart antennas and a beamforming processing over each sub-carrier. The SINR variate $\gamma_k = \gamma(H_k, \gamma)$ depends only on the channel variations over k , whereas the interference pattern γ does not vary along the data region. Assuming the perfect knowledge of $\{H_k, Q\}$, the minimum variance distortionless receiver (MVDR) issued to combine the signals received at different antennas, yielding at the output of the combiner the following SINR,

$$\gamma_k = \frac{p_o}{N_T} \text{tr}\{H_k^H Q^{-1} H_k\} \quad (3)$$

to be exploited when establishing the branch metric of the Viterbi decoder.

D. Randomized interference scenario

This scenario is modeled to exploit the maximum diversity provided by the fluctuations of both channel and impairments. Diversity is artificially introduced through the randomized multi-user access approach which provides interference fluctuation over the codeword. In this case, any interference mitigation techniques are unfeasible due to the unpredictability of the impairments configuration (i.e., the highly varying covariance Q_k cannot be reliably estimated). To exploit the diversity provided by the MIMO channel we adopt an OSTBC with antennas sufficiently spaced apart. The receiver is based on coherent maximum likelihood (ML) OSTBC detector, where the Viterbi decoder exploits the knowledge of the average noise power σ^{-2} over the whole data region (conventional decoder). In this case, the SINR to be used for decoding is

$$\gamma_k = \frac{p_o}{N_T} \frac{\text{tr}\{H_k^H Q^{-1} H_k\}}{\sigma^2} \quad (4)$$

As lower-bound performance reference, we also consider the optimal decoding based on the knowledge of the instantaneous interference power σk^2 on each subcarrier for this genie decoder the instantaneous SINR at the decision variable is

$$\gamma_k = \frac{p_o}{N_T} \frac{\text{tr}\{H_k^H Q^{-1} H_k\}}{\sigma k^2} \quad (5)$$

The channel and the interference are modeled for analytical purposes, it is convenient to rewrite the SINR as a function of the $N_T N_R \times 1$ normalized space-frequency channel vector

$$\hat{h}_k = \sqrt{\frac{p_o}{N_T}} \cdot \text{vec}(Q_k^{-H/2} H_k) \quad (6)$$

Where the interference covariance is $Q_K = Q$ defined as in (1) for the coordinated scenario, $Q_K = \sigma^2 I_{NR}$ for the randomized one with conventional decoder and for the genie decoder. The SINR reduces to:

$$\gamma_k = \|\hat{h}_k\|^2 \quad (7)$$

Properties of this equivalent space-frequency channel \hat{h}_k for performance analysis depend on the spatial-temporal dispersion of the multi-path propagation for the MIMO channel H_k , the spatial configuration of the inter-cell interference from the covariance Q_k and the fluctuations of the interference power induced by the multiple access policy (i.e., the variations of γk), according to the models in the previous sections.



3. PROPOSED BIT SPARSE CODING

In the sequel we extend the performance evaluation to higher order modulations. Without loss of generality, we consider a fixed interference scenario, dropping the symbol γ in the notation. We focus on a MQAM modulation, with a modulation set of dimension defining the transmitted symbols as,

$$s_k = (s_k^Q + js_k^I)\sqrt{E_g} \text{ with } s_k^Q, s_k^I \in \{\pm 1, \pm 3, \dots, \pm\sqrt{M}-1\}$$

$$\text{Where } E_g = \frac{3}{2(M-1)}$$

is the transmitted waveform energy. We restrict the analysis to BICM with Max-Log-Map demodulation. Compared to the error probability derivation, here the average PEP for an error event of Hamming distance depends not only on the subcarriers, but also on the symbols of the M-QAM constellation and the positions in the bit labels that are associated with the erroneous bits. More specifically, let us consider the h bit the interleaver maps such a bit to a constellation symbol on the sub-carrier and to a position in the modulation label set. We can express the interleaver effect by writing the sets, $L = \{l_1, \dots, l_d\}$ and $\chi = \{x_1, \dots, x_d\}$. We point out that the transmitted symbol $x_k \in S$ depends not only on the bit in l_k but also on the remaining $m-1$ bits of the label. They are selected (by the interleaver) from different positions of the same coded block, thus we can consider the other $m-1$ bits as independent variables. We further suppose that each bit of the error event is assigned to a different frequency: $f_i \neq f_j$ for $i \neq j$ where $\{i, j\} = 1, \dots, d$. This is a simplification as an interleaver (acting on a finite length coded sequence) can associate to the same frequency two or more erroneous bits of the same error event. The average PEP can be obtained as,

$$P(c) \leq \sum_L P(\chi) P(c|L, \chi) \quad (8)$$

Where $P(c|L, \chi)$ is the PEP conditioned to the set (L, χ) , while $P(L) = 1/m^d$ is the probability of each label set. Notice that for any coded bit sequence to be modulated and any given label set L , there are $2^{(m-1)d}$ possible symbol sequences χ with equal probability $P(\chi) = 1/2^{(m-1)d}$. As in the BPSK case, the conditioned PEP $P(c|L, \chi)$ depends on the effective SINR γ_{eff} that is a linear combination of the SINR values $\gamma_f = \{\gamma_{f_1}, \dots, \gamma_{f_d}\}$. Here, however, each SINR value γ_k has to be scaled by a factor to account for the Euclidean distance between the transmitted symbol and its nearest concurrent in the considered symbol constellation, hereinafter denoted as Δ_k^2 . This factor can vary with x_k and l_k . More specifically, for a QAM modulation, let S_0^1 and S_1^1 be the subset of all symbols x_k whose label has the value 0 (and 1) in position l_k , for $l_k = 1$. The subset S_2^1 focusing on the d^{th} bit of the received code word, accounting for $M=16$ with Gray's mapping. If the transmitted bit is equal to 1 and it is mapped onto the l th label position, the transmitted symbol x_k belongs to the subset S_1^1 . The Max-Log-Map

demodulator decision is erroneous when the received symbol lies in S_0^1 . Thereby, the probability of error can be upper bounded by using the Euclidean distance between x_k and the boundary of the area associated to the nearest neighbor in S_0^1 . For the 16-QAM example ($d=2$), this distance is $\sqrt{E_g}\Delta_k$, with $\Delta_k=1$ for ever. The k th coded bit is mapped over the frequency in the QAM symbol and in the label position. The plot below shows the areas of correct decision for the k th bit. Symbols x_k , therefore this value does not depend on the other $m-1$ bits. The same holds for label position $l=4$. On the other hand, for label positions $l=1$ and $l=3$ the value of the scaled distance is $\Delta_k=1$ for half symbols and $\Delta_k=2$ for the other half symbols. It follows that the k th bit experiences the SINR:

$$\gamma_k = \frac{P_0}{N_T} \frac{3}{2(M-1)} \Delta_k^2 \|\hat{h}_k\|^2 \quad (9)$$

The modified expression is used to rewrite the effective SINR (16) as a function of the set of d Euclidean distances $\{\Delta_1, \dots, \Delta_k\}$. Thereby the corresponding PEP becomes:

$$P(c|L, \chi) = P(c|D) = E_\gamma [Q(\sqrt{2\gamma_{\text{eff}}(\gamma, D)})] \quad (10)$$

It is worth noticing that each distance Δ_k can assume only few values. As a matter of fact, for the 16-QAM constellation it is $\Delta_k=1$ for three quarters of the sets and $\Delta_k=3$ for the remainder, i.e.: $(\Delta_k=1) = 3/4$ and $(\Delta_k=3) = 1/4$. Similar considerations hold for 64-QAM whereas it can be easily observed that for QPSK ($n=4$) it is $\Delta_k=1$ and the effective SINR simplified. For BPSK modulation it is $\Delta_k=1/2$. Since only few distance values are observed, it is convenient to gather all the configurations that correspond to the same distance set c , yielding:

$$P(c) = E_\gamma [P(c|D1)] \quad (11)$$

Where $p(D)$ is the probability of the distance set c . However, in order to avoid the expensive EVD for each configuration of we propose to approximate the expectation by means of a sample average: we simulate some values as the outcomes of i.i.d. random variables, having known distribution (see the probabilities above for 16-QAM); for each value, the effective SINR is obtained and its pdf is calculated. The estimate of the average bit error probability is then obtained by averaging over some realizations.

4. SIMULATION RESULTS

This section gives the performance evaluation of the proposed method under various regards.

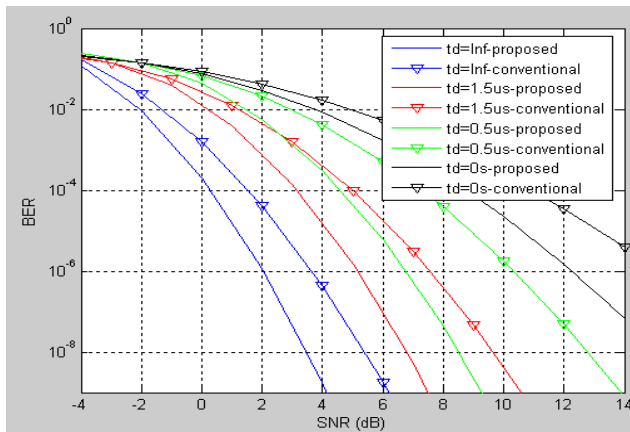


Figure-1. Performance of the proposed method at various Doppler frequencies.

The above figure represents the Bit error rate versus Signal to noise ratio plot. From the above figure it is clear that the performance of the proposed method for various Doppler effects (1ns, 1.5us, 5us, 0us) is efficient. It also denotes that with an increase in SNR value at there is a nominal decrease in the BER of the proposed method is decreasing due to the availability of multiple channels, thus the total SINR is going to be decreased. Thus, this decreased value provides the optimum power allocation for users.

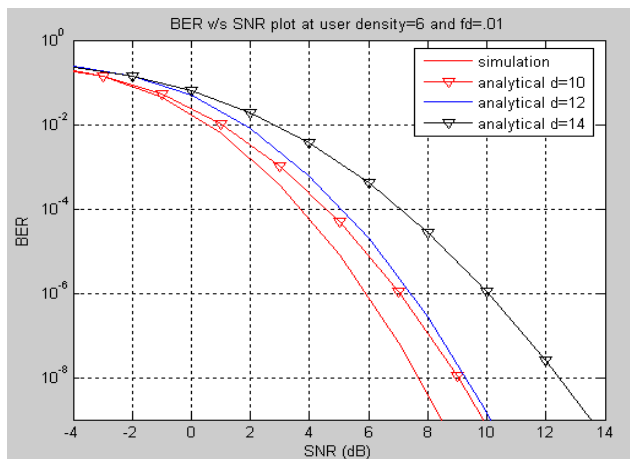


Figure-2. Analytic and simulated BER Vs traffic load in randomized 3interference scenario with an ideal genie decoder.

Performance of a SISO IEEE802.16-e system with QPSK, convolution code WiMAXcc1, Interferencerandomization with PUSC strategy and fixed delay spread $\sigma_{\tau}=1\mu s$.

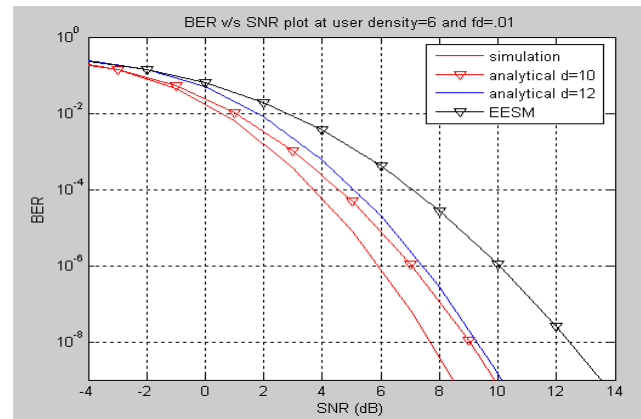


Figure-3. BER Vs SINR in coordinated interference scenario for the proposed.

Above Figure-3 shows the comparison between the two methods for the IEEE 802.16-d beam forming scenario with QPSK modulation and codeWiMAXcc1. Conclusions are described in the next section.

5. CONCLUSION

An estimation logic in MIMO system following OFDM approach is developed. The Error performance of the developed approach is observed to be minimized under the coordinated interference scenario and randomize interference scenario. The signal estimation is improved using bit spring logic. The overall performance was proved to be optimal under channel diversity condition, for random as well as a coordinated interference model.

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