



AREAS CATEGORIZATION BY OPERATING SUPPORT VECTOR MACHINES

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ABSTRACT

In recent years, Support Vector Machines (SVMs) have demonstrated excellent functioning in a variety of area categorization problems. This paper explains areas categorization by operating SVMs. The SVM is an ideally excellent machine learning approach with abundant outcomes in categorization of high dimensional datasets and has been discovered reasonable performance with the elite machine learning procedures. In the past, SVMs have been verified and assessed only as pixel-based image classifiers. Moving from pixel-based methods concerning object-based illustration, the dimensions of distant detecting imagery feature space increases considerably. These outcomes increase the difficulty of the categorization process, and instigate complications to conventional sample-based categorization systems. The goal of this paper is to estimate SVMs for usefulness and outlooks for object-based area categorization as a contemporary computationally best technique. SVM method for multi-class categorization was followed, built on basic image objects yields by a multi-resolution subdivision algorithm. The subdivision procedure constructed primitive objects of capricious sizes and figures. Then, a feature assortment step took place in order to deliver the features for categorization, which involved spectral, texture and shape information. Contextual evidence is not utilized. Following the feature assortment phase, a module combining SVM classifier and the subdivision procedure was established in C++ and built on DHTML for feature illustration. For training the SVM, example image objects, imitative from the subdivision technique are utilized. The SVM method appears very capable for object centred image analysis and future effort will emphasis on the combination SVM classifiers with rule-based classifiers.

Keywords: pixel-based image classifiers, support vector machines, subdivision procedure, feature assortment.

1. INTRODUCTION

1.1 Image analysis

IN contemporary years, research has developed in computer prophecy approaches useful to remotely sensed images such as subdivision, object oriented and knowledge-based approaches for categorization of high-resolution imagery [1]. In Computer Prophecy, image investigation is studied in three levels: low, medium and high [1]. Such methods were normally applied in distinct software environments meanwhile low and medium level procedures are procedural in type, though elevated levels is inferential and consequently for the first one wish procedural languages while for the second an expert system environment is more appropriate. New methods have been developed, newly in the arena of remote sensing. Some of them were based on knowledge-based methods in order to take benefit of the expert experience originated from human photo-interpreters [2]. In specific within an expert system environment, the categorization step has been applied through rationality procedures and heuristics, working on classes and attributes, which were applied by the user through an object-oriented illustration [3, 4]. This object-oriented illustration is essentially built on the image semantics and the precise understanding of the human specialist. In order to categorize each element of the image into the suitable class, the knowledge-based proficient system signified the explanations of the classes through rules and heuristics, which an expert clearly announces and cultivates within the system. As an outcome, more complicated approaches for image

categorization have been employed and numerous more image attributes can be expended for the categorization phase [5]. Very newly a new approach called object oriented image analysis is presented, integrating low-level, knowledge-free subdivision with high-level, knowledge-based fuzzy categorization techniques.

2. COMPUTATIONAL APPROACHES

Other fields of artificial intelligence have also been grown such as computational intelligence and machine learning including neural networks, fuzzy systems, genetic algorithms, intelligent agents and SVMs [6]. Machine learning is an essential part of pattern recognition, and in particular categorization [7]. Given that in the past, digital remote sensing used pattern recognition techniques for categorization purposes, modern machine learning techniques have been also applied for remote sensing purposes and succeeded very decent categorization outcomes [8]. The SVM is a hypothetically excellent machine learning system with abundant outcomes in the categorization of high-dimensional datasets and has been discovered reasonable with the best machine learning procedures. In the past, SVMs were verified and assessed only as pixel cantered image classifiers with very decent outcomes. Additionally, for remote sensing statistics it has been indicated that SVMs have pronounced potential, particularly for hyper spectral statistics, due to their high-dimensionality. In modern reports, SVMs were compared to other categorization approaches, such as decision tree classifiers, maximum likelihood, nearest neighbour and neural networks, for



remote sensing imagery and have surpassed all of them in strength and precision [9].

3. OBJECTIVES

The primary objective of this study is to assess SVMs for their usefulness and prospects for area categorization. A secondary objective is to assess the precision of SVM related to easier and extensively use categorization methods such as Nearest Neighbour classifier. Also, the computational effectiveness and training size needs of SVMs were set for attention.

4. APPROACH

4.1 Subdivision

Image subdivision is an essential part of object-based image analysis approach [10]. The digital image is no longer considered as a lattice of pixels, but as a collection of primitives and similar areas, called primitive image objects. The object-oriented illustration affords to the categorization procedure knowledge that could not be originated from single pixels such as framework and structure knowledge. These are very significant features to photo analysis and image accepting [11]. Objects can be cleverer than pixels, in a sense of knowing their “neighbors” and the spatial or spectral relations with and among them. In order to accomplish object-based categorization, a subdivision procedure is required to specify knowledge-free basic image objects. When a specialist conducts a photo analysis task, the scale of imagery is indicated by the nature of image semantics to be recognized [11]. During the higher-level image categorization phases, there is a requirement to have fundamental objects of various dimensions and preferably on various scales of perception obtained from the similar imagery [12]. That is the foremost reason to use remote sensing image categorization; a multi-resolution subdivision method is required. For this study effort the MSEG multi-scale subdivision procedure was used [12]. The key reason for this choice was that it has an open construction to implement new features in Java. Adaptive neighborhood subdivision methods effort to overcome problems, such as background objects may even seem brighter but implementation issues such as neighbourhood dimensions and the resolve of areas where background objects are brighter. It useful to resolve problems related to pose difficult problem. These troubles are determined by operating a multistage subdivision technique and the subsequent thresholds are mapped operating pseudo-colour image treating techniques to improve human visualization. For estimation and determinations, the multi-resolution subdivision procedure in eCognition is also used. MSEG can be termed as an area amalgamation process. The first primitive object representation is the single image pixel. Through iterative pair wise object fusions, which are made at several iterations called passes, the final segmentation is achieved. The principle for object amalgamation is a similarity cost measure, defined as object heterogeneity, and computed built on spectral, texture and structure features for each probable object

merge. The dissimilarity is then related to a user-defined limit, named scale parameter to determine the decision of the combine. MSEG also deals a multi-resolution process, which does subdivisions at numerous levels and at the same time offers automatic topology of objects within each level and among levels [12].

Multistage method uses two phases. The first phase employs a multistage-programmed threshold estimator built on histogram moments to division the image at different stages. The second phase changes the segmented image operating pseudo-colour mapping to yield a colour image. Adaptive neighbourhood segmentation methods attempt to overcome drawbacks such as contextual objects appearing brighter, but implementation issues such as neighbourhood sizes and the determination of regions where background objects are brighter still pose a difficult problem. These problems are resolved by using a multistage segmentation method and the subsequent thresholds are plotted using pseudo-colour image processing methods to improve individual visualization.

4.2 Scientific summary of MSEG

This portion delivers the explanations and the scientific synopsis of MSEG.

Definition 1

Given a histogram with two approaches a and b, the subdivision error can be reduced by minimizing the cost function,

$$e = \sum_{k=0}^{K-1} \sum_{n=0}^{N-1} (f(k, n) - a)^2 (f(k, n) - b)^2 \quad (1)$$

Where $f(k, n)$ is the image, n is the number of pixels in the region k , a , b are image constraints which can be calculated by c_1 and c_2 .

Definition 2

The r^{th} moment M_r is expressed as

$$M_r = \frac{1}{N} \sum_{k=0}^{K-1} \sum_{n=0}^{N-1} g(k, l)^r = \frac{1}{N} \sum_{i=0}^{P-1} h(i) i^r \quad (2)$$

Where $N=KL$ is the absolute number of pixels in the image, $h(i)$ is the i^{th} histogram value which is the number of pixels which have $f(k, n)=i$, and P is the number of grey levels.

Definition 3

The central moment I_r of the histogram are defined as



$$I_r = \frac{1}{N} \sum_{k=0}^{l-1} \sum_{n=0}^{s-1} (g(m, n) - n)^s \quad (3)$$

$$= \frac{1}{N} \sum_{j=0}^{P-1} h(j)(k - n)^s \quad (4)$$

where $s = 1, 2, \dots$ and n is the mean of the distribution.

- I_1 is the main histogram mean of the distribution.
- I_2 is known as the variance and gives the measure of gray level difference.
- I_3 is the measure of the skewness of the histogram. Further information on the derivation, analysis and properties of central moments can be obtained from the book by Gonzalez.

Minimization of the segmentation error using the cost function in Equation (1) gives

$$b = \frac{d_1 - \sqrt{d_1^2 - 4d_2}}{2} \quad (5)$$

$$c = \frac{d_1 + \sqrt{d_1^2 - 4d_2}}{2} \quad (6)$$

Where

$$d_1 = \frac{I_3 - I_1 I_2}{I_2 - I_1^2} \quad (7)$$

$$d_2 = \frac{I_1 I_3 - I_2^2}{I_2 - I_1^2} \quad (8)$$

The threshold value is given by

$$T = 0.5(a + b) + m \quad (9)$$

Let us study the kind of T in equation (9). The deviation of a threshold value T from the mean of the distribution m depends exclusively on the parameters a, b . Consider the following theorem.

Theorem 1

If an image has constant intensity, the central moments

$$I_r = 0 \quad \text{for } r \geq 1.$$

From equation (3),

$$I_r = \frac{1}{N} \sum_{k=0}^{M-1} \sum_{n=0}^{P-1} (g(l, m) - n)^s \quad (10)$$

Meanwhile the image has constant intensity, $g(l, m) = n$ and therefore $I_r = 0$ for $r \geq 1$. Note also

that $(a + b) = 0$ since both c_1 and c_2 are zero, therefore the threshold value, which minimizes the subdivision error, is m .

4.3 Multistage subdivision and improvement

The scientific basis presented above can be iteratively used to automatically produce threshold values $S_j, j = 0, \dots, q$ for multistage subdivision. For such an automatic procedure, the subsequent convergence standards are needed.

$$(1) S_j > R - 1.$$

The threshold value is superior to the maximum pixel intensity.

$$(2) S_j < S_{j-1}.$$

In practice, this hardly occurs. This would happen if $(b + c) < 0$, and this case is treated below.

(3) $(b + c) < 0$. We note from theorem 1 that n is the threshold value for an image with constant intensity. Equations (5) and (6) demonstrate that $(b < c)$, and from equation (1), both $(b, c) \geq 0$. If $(b + c) < 0$ then $(b < 0)$ which contradicts equation (1) and multistage subdivision terminates.

Algorithm 1

1. Compute the histogram $h[i]$,
 $i = 0, \dots, P-1$ of $f(l, k)$.
2. $S_0 = 0.5(b + c) + n$
3. If $(S_j > Q - 1)$ or $(b + c) < 0$
or $(S_j > S_{j-1})$
goto step 7 else goto step 4.
4. $N_r = \frac{1}{W} \sum_{i=S_j}^{Q-1} h(i)(i - n)^s$,
where W is the number of pixels
in the image with grey level $i \geq T_j$.
5. $S_{j+1} = 0.5(b + c) + n$.
6. Goto step 3.
7. exit

Nevertheless, for a correct subdivision, histogram post processing is needed. An adaptive histogram equalization technique is used to properly allocate pixels to their correct classes defined by the thresholds. To subdivision at threshold value S_j , histogram equalization

is useful in the interval S_{j-1} to S_{j+1} before segmenting.

This is built on the observation that intensity values may sometime be higher at the center of lesions and



progressively declines outwards to the boundary and spikes. This process, hence efforts to subdivision the cancer and spikes into the same class. This can be viewed as region developing.

Minimization of defective subdivision is achieved by an adaptive histogram equalization method. Though, noise appears as spike-like regions, which can be eliminated on the basis of size. The human visual system can only discern a limited number of gray scales. Therefore, representing the results from multistage subdivision in gray scale mode does not occur.

5. SUPPORT VECTOR MACHINES

Recently, SVMs have been a capable instrument for area categorization. Its fundamental idea is to represent data into a high dimensional space and find a splitting hyper plane with the greatest boundary. SVMs have frequently been discovered to deliver improved categorization outcomes that other widely used pattern recognition approaches, such as the maximum likelihood and neural network classifiers [7, 13]. Thus, SVMs are very attractive for the categorization of remotely sensed data. The SVM method requests to find the best splitting hyper plane between classes by concentrating on the training images that are located at the edge of the class descriptors.

These training images are called support vectors. Training images other than support vectors are rejected. This way, not only is a best hyper plane fitted, but also less training samples are efficiently used; thus high categorization correctness is attained with lesser training sets [14]. This attribute is very beneficial, especially for remote sensing images and more precisely for object-based image analysis, where object samples tend to be fewer in number than in pixel centered methods. A complete formulation of SVMs can be discovered at a number of journals [7, 15, 16, 17]. Here, the fundamental ideologies will be offered and then their implementation and application to object based image analysis will be assessed. Let us study a controlled binary categorization problem. If the training statistics are characterized by $\{x_i, y_i\}$, $i = 1, 2, \dots, N$, and $y_i \in \{-1, +1\}$, where N is the number of training samples, $y_i = +1$ for class ω_1 and $y_i = -1$ for class ω_2 . Suppose the two classes are linearly separable. This means that it is possible to find at least one hyper plane defined by a vector w with a bias w_0 , which can separate the classes without error:

$$g(x) = u \cdot x + u_0 = 0 \quad (11)$$

To find such a hyper plane, u and u_0 should be assessed in a way that $\pm 1 \leq y_i(u \cdot x + u_0)$ for $y_i = +1$ (class ω_1) and $y_i(u \cdot x + u_0) \leq \pm 1$ for $y_i = -1$ (class ω_2). These two, can be combined to provide equation 2:

$$0 \leq y_i(u \cdot x_i + u_0) - 1 \quad (12)$$

The objective is to examine for the hyper plane that leaves the maximum boundary between classes. To be able to find the best hyper plane, the support vectors must be defined. The support vectors lie on two hyper planes, which are parallel to the optimal and are given by:

$$y_i(w \cdot x_i + w_0) = \pm 1 \quad (13)$$

If a simple rescale of the hyper plane constraints w and w_0 takes place, the margin can be articulated as

$$\frac{2}{\|v\|}$$

discover the best hyper plane:

$$\text{Minimize } \frac{1}{2} \|v\|^2 \quad (14)$$

$$\text{Subject to } 0 \leq y_i(v \cdot x_i + w_0) - 1$$

$i = 0, 1 \dots N$. Using a Lagrangian formulation, the above problem can be translated to: Maximize

$$\sum_{i=1}^N z_i - \frac{1}{2} \sum_{i,j=1}^n z_i z_j y_i y_j (x_i \cdot x_j) \quad (15)$$

Subject to

$$\sum_{i=1}^N z_i y_i = 0 \quad \text{and} \quad z_i \geq 0 \quad i = 1, 2, \dots, n \quad \text{where } z_i \text{ are the}$$

Lagrange multipliers. Under this formulation, the optimal hyper plane discriminant function becomes:

$$g(x) = \sum_{i \in S} z_i y_i (x_i \cdot x) + u_0 \quad (16)$$

Where S is a subset of training samples that correspond to non-zero Lagrange multipliers. These training samples are called support vectors. In most cases, classes are not linearly separable, and the condition of equation 12 cannot be satisfied. In order to handle such cases, a cost function can be expressed to combine maximization of boundary and minimization of error conditions, operating a set of parameters called slack parameters π which finds the error of the hyper plane fitting. This cost function is defined as: Minimize

$$J(u, u_0, \pi) = \frac{1}{2} \|u\|^2 + c \sum_{i=1}^N \pi_i \quad (17)$$

$$\text{Subject to } y_i(u \cdot x + u_0) \geq 1 - \pi$$



To streamline the above technique to non-linear discriminator functions, the SVM plots the input vector x into a high-dimensional feature space and then builds the best isolating hyper plane in that space. One would study that representing into a high dimensional feature space would add additional complication to the problem. But, according to the Mercer's theorem [7], the inner product of the vectors in the mapping space can be expressed as a function of the inner products of the corresponding vectors in the original space. The inner product operation has an corresponding illustration:

$$\phi(x)\phi(z) = k(x, z) \quad (18)$$

Where $K(x, z)$ is named as kernel function. If a kernel function K can be discovered, this function can be used for training without knowing the precise form of ϕ . The dual optimization problem is now formed as Maximize

$$\sum_{i=1}^N z_i - \frac{1}{2} \sum_{i,j=1}^n z_i z_j y_i y_j (x_i \cdot x_j) \quad (19)$$

subject to

$$\sum_{i=1}^N z_i y_i = 0 \quad \text{and} \quad z_i \geq 0 \quad i = 1, 2, \dots, N$$

The resulting classifier becomes:

$$g(x) = \sum_{j \in S} z_j y_j k(x, x_j) + w_0 \quad (20)$$

6. CLASSIFICATION

For utilizing SVM to multi-class categorizations, two main approaches have been proposed. The fundamental idea is to decrease the multi-class to a set of binary problems so that the SVM approach can be used. The first method is called "one against all". In this method, a set of binary classifiers is trained to be able to isolate each class from all others. Then each data object is catalogued to the class for which the biggest decision value was determined. This technique trains n SVMs (where n is the number of classes) and there are n decision functions. Although it is a fast technique, it experiences from mistakes caused by slightly imbalanced training sets. Another method was newly presented, which is analogous to the "one against all" method, but uses one optimization problem to get the n decision functions (equation 20). Reducing the categorization to one optimization problem may need fewer support vectors than a multi-class cataloging based on several binary SVMs. The second method is called "one against one". In this, a sequence of classifiers is employed to each pair of classes, with the best normally calculated class kept for each object. Then a max-min operator is used to determine to which class the object will be ultimately allocated. The claim of this technique needs $n(n-1)/2$ machines to be employed. Even if this technique is more computationally challenging than the "one against all" technique, it has been displayed that

it can be more appropriate for multi-class categorization problems, thus it was chosen for SVM object-based image categorization.

6.1 Implementation

In order to employ the SVM approach for object-based image analysis, it is essential to accomplish a subdivision of the image. The SEGM procedure was chosen to accomplish subdivision at many scales [12] and to yield basic image objects to be used for SVM categorization. For the basic objects, to be usable by a categorization procedure, there is a need to apply an interface between image objects and the classifier. This interface should include an object feature export mechanism and also a method to deliver training data for the classifier. An extra component is applied into the SEGM key library to add the functionality of choosing example objects. Since an assessment was to be made with the nearest neighbor classifier used in eCognition, a TAT Masquerade import component is also employed, so that the training object assortment procedure would be as transparent and objective as possible. For the object attribute interface, the HTML language is chosen, so that open principles are obeyed. A HTML illustration is applied for the subdivision level class, to deliver the classifier all the evidence about the subdivision procedure that was achieved to yield the object primitives. A commonly utilized SVM library called SVMLIB is then altered to be able to handle HTML level files as well as training examples from the SEGM procedure. A classifier component is then applied as an adapted version of SVMLIB. The suggested object-based image analysis technique operated in the succeeding way: A subdivision procedure was carried out with scale, color and figure variables. The properties of the basic objects were then calculated and transferred to HTML format. A TAT mask file along with its attribute table was introduced to the system and training object examples were defined. A training set of feature vectors was transferred from the SEGM procedure and is utilized for training the SVM module. The SVM component is capable of using 4 types of kernels for training and categorization:

Linear kernel $K(x,y)=xy$

Gaussian kernel $K(x,y)=\exp(-\gamma\|x-y\|^2)$

Polynomial kernel $K(x,y)=((x,y)+1)^d$

Sigmoid kernel $K(x,y)=\tanh(K(x,y)+1)$

where γ , r and d are kernel parameters.

All the above kernels follow Mercer's formula and can be utilized for mapping the feature space into a higher dimensional space to discover the best dividing hyper plane. In literature, there have been numerous comparison reports between the most common kernels [9, 14]. For pixel-based categorization of remotely sensed data, it has been exposed that native kernels such as RBF can be very efficient and precise. Also, the linear kernel is a special case of the RBF kernel, with specific variables. Built on the above, for the present study only RBF kernels are used. For the training of the SVM classifier, the error



variable e (equation 7) and the kernel variable γ had to be found. In order to discover the best variables for the RBF kernel function a cross-validation process was followed. Image object characteristics are included to be used by a classifier. Here only few of the existing characteristics are used. First the training set is scaled to the range of $[-1, +1]$ to elude attributes in better numerical ranges controlling

those in smaller ranges [6]. Then, the training set was separated to many smaller sets of equal size. Consecutively each subset was tested using the classifier trained by the remaining subsets. This way each image object is predicted once during the above process. The overall accuracy of the cross-validation is the proportion of appropriately categorized image objects.

Table-1. Nearest Neighbor - confusion matrix. The overall accuracy is 82.6%.

	Forestland	Grassland	Impervious	Water
Forestland	18952	4385	383	0
Grassland	2674	13845	184	0
Impervious	139	777	7539	0
Water	80	0	0	5740

After the cross-validation delivered the best variables for the SVM classifier, the training set is utilized to train the SVM. Then the classifier is delivered with all image basic objects so to derive the final object based categorization. The output of the above technique was a categorization map as well as an updated HTML illustration of the subdivision level.

7. DISCUSSION OF RESULTS

For the assessment of the established method, a Landsat TM image is used. The training samples in both cases were the same (a TAT mask file) and were found by the eCognition user guide for objective assessment. The original Landsat TM image and the training examples are offered in Figure-3. A reference dataset was also derived by photo-interpretation and is used to calculate confusion matrices (Figure-1).

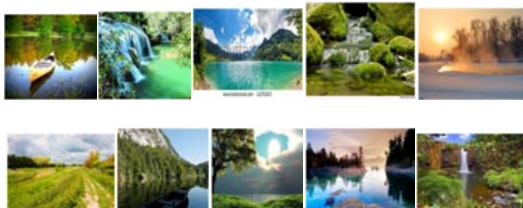


Figure-1. First row: the original Landsat TM image.
Right: The training set of class samples.



Figure-2. The ground-truth dataset used to evaluate results.

First, the training samples were projected upon small primitive objects. A cross-validation procedure was followed to provide the best C and γ parameters for the SVM classifier. The results of cross-validation are shown in Figure-4. The overall accuracy of the object-based SVM classification was 80.6% (Figure-2, Tables 1 and 2).



Figure-3.Left: Classification result with Nearest Neighbor.

Right: MSEG classification result with SVM. Training sample overlap with objects set to 50%.

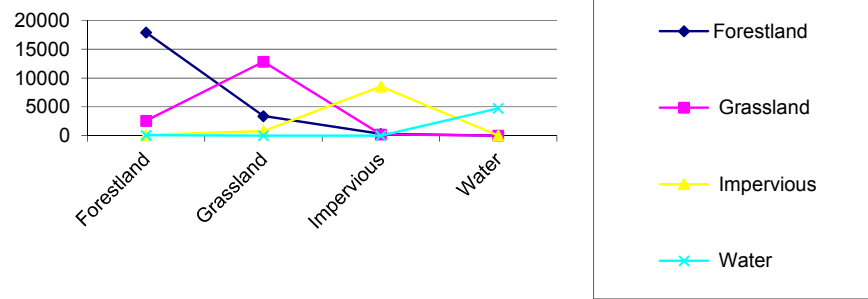


Figure-4. At accuracy 82.6 (Table-1).

Table-2. SVM -confusion matrix. The overall accuracy is 89.5%.

	Forestland	Grassland	Impervious	Water
Forestland	17843	2056	54	74
Grassland	734	15934	210	91
Impervious	234	221	8404	236
Water	170	23	20	4532

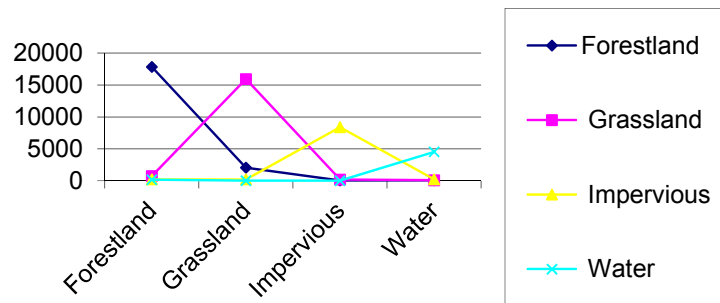


Figure-5. At accuracy 89.5 (Table-2).

Table-3. Nearest Neighbor confusion matrix. The overall accuracy is 82.1%.

	Forestland	Grassland	Impervious	Water
Woodland	16812	3452	280	220
Grassland	3541	15506	178	60
Impervious	251	321	7539	125
Water	445	851	3	4623

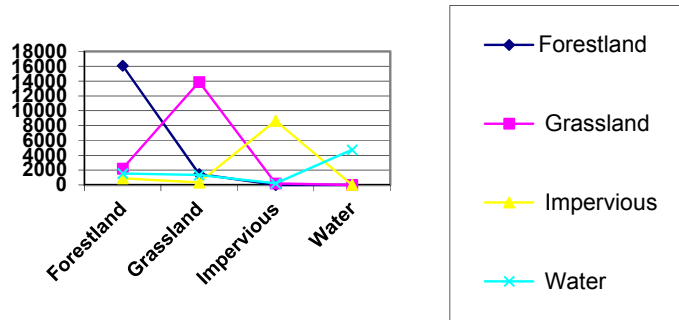


Figure-6. At accuracy 82.1(Table-3).



Figure-7. Categorization outcomes with nearest neighbour. Right: SEGM categorization outcomes with SVM.

In both classifications, errors have been introduced to the training sets for generalization evaluation. Then, in order to test the generalization ability of both classifiers, an error was introduced into the training samples, in the form of not using a minimum overlap restriction for sample object selection. This way, more training objects were selected with errors derived from the segmentation procedures. An interesting observation was that the SVM behaved better than the NN to the second training set and provided better classification results (Tables 3 and 4) giving an overall accuracy of 86.0% against 84.1% for the NN. Both classification results are presented in Figure-6.

Table-4. SVM confusion matrix. The overall accuracy is 85.0%.

	Woodland	Grassland	Impervious	Water
Woodland	17843	2056	54	74
Grassland	734	15934	210	91
Impervious	234	221	8404	236
Water	170	23	20	4532

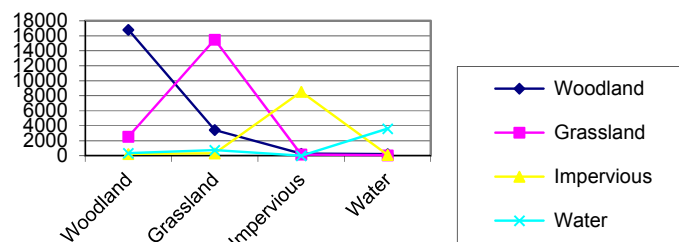


Figure-8. At accuracy 85.0(Table-4).

8. DEDUCTIONS AND FUTURE WORK

Overall, the SVM categorization method was discovered very promising for object-based image analysis. It has been revealed that it can yield similar or even enhanced outcomes than the nearest neighbour for supervised categorization. The computational

effectiveness of SVM is great, with only a few minutes of runtime is necessary for training. This is hypothetically anticipated but also, the employment in Java is very fast. However, extremely huge remote sensing datasets were not verified. An extremely decent attribute of SVMs is that only a little training set is required to deliver very decent



outcomes, as only the support vectors are of importance during training. Future effort will incorporate association of many SVM kernels for object oriented image categorization. Also, an incorporation of SVM classifiers with rule-based classifiers will be applied for context-based categorization.

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