



# ENHANCED SECURITY FOR DATA TRANSACTION WITH PUBLIC KEY SCHNORR AUTHENTICATION AND DIGITAL SIGNATURE PROTOCOL

M. Mesran<sup>1</sup>, Muhammad Syahrizal<sup>1</sup> and Robbi Rahim<sup>2</sup>

<sup>1</sup>Department of Informatics Engineering, STMIK Budi Darma, Medan, Indonesia

<sup>2</sup>School of Computer and Communication Engineering, Universiti Malaysia Perlis, Malaysia

E-Mail: [usurobbi85@zoho.com](mailto:usurobbi85@zoho.com)

## ABSTRACT

Authentication and digital signatures need to be done to identify each other in communication, the Schnorr scheme algorithm is an algorithm that can be used for authentication and digital signatures, this paper provides an understanding of how authentication and digital signatures work to make it easier for readers to know the application Schnorr algorithm on information security process, and the result show the message was more secure from any attacker.

**Keywords:** authentication and digital signatures, secure communication, Schnorr Scheme, application schnorr.

## INTRODUCTION

Authentication is an identification by each communicating party, meaning that some communicating parties must identify each other (Wang & Song, 2016) (Chakraborty, Rahman, & Rahman, 2016) (Rahim, Man-In-The-Middle-Attack Prevention Using Interlock Protocol Method, 2017). Information obtained by a party from another party should be identified to ensure the authenticity of the information received (Chakraborty, Rahman, & Rahman, 2016). Identification of information can be the date of making information, information content, time of delivery and other matters relating to that information. Message authentication is successful in protecting both parties from exchanging messages from third parties (Sravanthi & Prasad, 2011). However, message authentication cannot prevent the possibility of both sides attacking each other. In situations where there is no complete trust between the sender and the recipient of the message, a mechanism is required rather than authentication (Wang & Song, 2016) (Sravanthi & Prasad, 2011). The most interesting solution to this problem is the digital signature (Wang & Song, 2016) (Sravanthi & Prasad, 2011) (Shiralkar & S. Vijayaraman, 2033). A digital signature is an authentication mechanism that allows the message maker to add code that acts as its signature. The signature ensures the integrity and source of a message (K. Doke & M Patil, 2012).

Claus Schnorr's authentication and digital signature scheme take securities from the problem of calculating discrete logarithms (Chakraborty, Rahman, & Rahman, 2016). This scheme uses prime numbers and modulo in the process of forming the key. The authentication scheme can modify into a digital signage scheme. The process of establishing the private and public keys is the same as the authentication scheme, only in the digital signature scheme added a hash function (Chakraborty, Rahman, & Rahman, 2016) (K. Doke & M Patil, 2012).

## THEORY

### Information security

Information Security is a protection against information when the information is sent from one system to another (Hariyanto & Rahim, 2016) (Legito & Rahim, 2017) (Nofriansyah & Rahim, 2016) (Rahim & Ikhwan, Cryptography Technique with Modular Multiplication Block Cipher and Playfair Cipher, 2016) (Rahim & Ikhwan, Study of Three Pass Protocol on Data Security, 2016) (Siahaan & Rahim, 2016). The information security system has four very basic goals, such as:

#### a) Confidentiality

Guarantee, whether the information sent, cannot be opened or cannot be known by others who are not eligible. For sensitive data, a high degree of confidentiality is required, which is only accessible to certain parties (the rightful party).

#### b) Integrity

Ensure the integrity and authenticity of data, so that the efforts of irresponsible parties to duplicate and destroy data can be avoided.

#### c) Availability

Ensures legitimate users to access their information and resources. The aim is to ensure that the proper parties are not rejected access to the information that they are entitled.

#### d) Legitimate use

Ensure certainty that the source not used or information not accessed by untrustworthy parties (unauthorized parties).

### Authentication

Authentication (Braz & Robert, 2006) (Guidorizzi, 2013) is a term applied in a broad sense. The word implicitly means more than conveying the idea that the tool has provided assurance that unauthorized parties are not manipulating information. Authentication is unique to the security topic; examples include access control, entity authentication, message authentication, data integrity, non-repudiation, and key authentication (Wang & Song, 2016)



(Chakraborty, Rahman, & Rahman, 2016) (Sravanthi & Prasad, 2011) (Guidorizzi, 2013).

Authentication is one of the most important things in information security. Until the mid-1970s, it remained thought that secrecy and authentication were closely connected. With the discovery of hash and digital signatures (Rahim, Dahria, Syahril, & Anwar, 2017), it continues recognized that confidentiality and authentication are separate and independent issues (K. Nair, Navin K.S, & Chandra C.S, 2015). At first, it did not seem important to separate them, but there were situations where they were not only useful but necessary (Shiralkar & S. Vijayaraman, 2033) (Haddaji, Ouni, Bouaziz, & Mtibaa, 2016) (Sadikin & Wardhani, 2016), the formulas used in the authentication process are as follows:

- a)  $r (r < q)$
- b)  $z = a^r \text{ mod } p$
- c)  $n = (r + se) \text{ mod } q$
- d)  $z = ((a^y).(v^e)) \text{ mod } p$

### Digital signature

A digital signature is an authentication mechanism that allows the message maker to add code that acts as its signature. The signature ensures the integrity and source of a message (Sravanthi & Prasad, 2011) (Mali, Mahalle, Kulkarni, Nangude, & Navale, 2017).

The digital signing of a document is the fingerprint of the document, and its timestamp is encrypted using the private key of the signing party (Ratha, Connell, & Bolle, 2001). The digital signature utilizes a one-way hash function to ensure that the signature applies only to the concerned document (Wang & Song, 2016) (Chakraborty, Rahman, & Rahman, 2016) (Rahim, Dahria, Syahril, & Anwar, 2017). The receiving party can check the validity of the digital signature.

### Schnorr algorithm

Claus Schnorr Authentication and Digital Signature scheme take securities from the problem of calculating discrete logarithms (Xin, Wang, Shao, Wang, & Zhang, 2015) (Cao & Markowitch, 2009). This scheme also uses prime numbers and modulo in its key forming process. The difficulty level for solving this algorithm is about  $2t$ , where this  $t$  value can be determined by itself (Cao & Markowitch, 2009).

The authentication scheme can be changed into a digital signature scheme. The process of establishing the private and public keys is the same as the authentication scheme, only in the digital signature scheme added a hash function (Xin, Wang, Shao, Wang, & Zhang, 2015).

### RESULT AND DISCUSSIONS

The Schnorr Authentication Protocol and Digital Signature Testing Process The protocol will be explained gradually in the following process, starting with the establishment of the key (Alice) as follows:

1. Alice selects  $p$ ,  $q$  and  $a$  as below:

$$p = 166853$$

$$q = 59$$

$$a = 56937$$

These values meet the requirements that:

- a.  $P$  and  $q$  are primes,
- b.  $\text{GCD}(q, p-1)$  should not be worth 1,
- c. The value of the operation  $(a^q) \text{ mod } p$  should be 1.

2. Alice selects the value of  $s (s < q)$ .

$$s = 58 \text{ (s are private key)}$$

3. Alice calculates the value of  $v$  with the following formula:

$$v = a^{(-s)} \text{ mod } p$$

$$v = 56937^{(-58)} \text{ mod } 166853$$

$$v = ((56937^{(-1)} \text{ mod } 166853)^{58}) \text{ mod } 166853$$

Complete the operation  $(56937^{(-1)} \text{ mod } 166853)$  with extended euclidean algorithm

$$(56937^{(-1)} \text{ mod } 166853) = 76260$$

$$V = (76260^{58}) \text{ mod } 166853 \text{ (finish with fast exponentiation)}$$

$$V = 56937 \text{ (v is the public key)}$$

The key that is formed will be used on the authentication process between Alice and bob; here is the process of authentication scheme with Schnorr algorithm:

1. Alice selects  $r$  value as follows:

$$r = 45$$

2. Alice calculates the value of  $x$

$$x = a^r \text{ mod } p \text{ (Finish with fast exponentiation)}$$

$$x = 56937^{45} \text{ mod } 166853$$

$$x = 94651$$

Alice sends  $X$  to Bob

3. Bob chose the  $e$  value as follows:

$$e = 3598229$$

Bob sends  $e$  to Alice

4. Alice calculates the  $n$  value as follows:

$$n = (r + se) \text{ mod } q$$

$$n = (45 + 58 \cdot 3598229) \text{ mod } 59$$

$$n = 49$$

Alice sends  $n$  to Bob

5. Bob did the following verification:

$$z = ((a^y).(v^e)) \text{ mod } p$$

$$z = ((a^y) \text{ mod } p \cdot (v^e) \text{ mod } p) \text{ mod } p$$

$$z = (56937^{49} \text{ mod } 166853) \cdot (56937^{3598229} \text{ mod } 166853) \text{ mod } 166853$$

$$z = (102788.166427) \text{ mod } 166853$$

$$94651 = 94651 \text{ (TRUE)}$$

The result of the operation  $((a^y) \cdot (v^e)) \text{ mod } p$  is equal to the value of  $z$ . The authentication process succeeded.

The next process is the process of digital signature scheme between alice and bob, here is the step with  $p$ ,  $q$ ,  $a$ ,  $s$  (private),  $v$  (public) is known:

$$p = 166853$$

$$q = 59$$

$$a = 56937$$

$$s \text{ (private)} = 58$$



$v(\text{public}) = 56397$

Message (M) = PENGUJIAN DIGITAL

1. Alice selects  $r$  value as follows:

$R = 21$

Alice calculates the value of  $z$

$z = a^r \bmod p$  (finish fast Exponentiation)

$z = 56937^{21} \bmod 166853$

$z = 153196$

2. Alice combines  $M$  and  $z$  and calculates the hash value:  $e = H(M, z)$

$M(1) = \text{ASCII from 'P'} = 80$

$(M(1), z) = M(1)$  Combined with  $z$

$(M(1), z) = 80153196$

$e(1) = H(80153196)$

$e(1) = 65565550$

$M(2) = \text{ASCII from 'E'} = 69$

$(M(2), z) = M(2)$  Combined with  $z$

$(M(2), z) = 69153196$

$e(2) = H(69153196)$

$e(2) = 67515350$

$M(3) = \text{ASCII from 'N'} = 78$

$(M(3), z) = M(3)$  Combined with  $z$

$(M(3), z) = 78153196$

$e(3) = H(78153196)$

$e(3) = 49665455$

$M(4) = \text{ASCII from 'G'} = 71$

$(M(4), z) = M(4)$  Combined with  $z$

$(M(4), z) = 71153196$

$e(4) = H(71153196)$

$e(4) = 69575053$

$M(5) = \text{ASCII from 'U'} = 85$

$(M(5), z) = M(5)$  Combined with  $z$

$(M(5), z) = 85153196$

$e(5) = H(85153196)$

$e(5) = 51536752$

$M(6) = \text{ASCII from 'J'} = 74$

$(M(6), z) = M(6)$  Combined with  $z$

$(M(6), z) = 74153196$

$e(6) = H(74153196)$

$e(6) = 69545551$

$M(7) = \text{ASCII from 'T'} = 73$

$(M(7), z) = M(7)$  Combined with  $z$

$(M(7), z) = 73153196$

$e(7) = H(73153196)$

$e(7) = 66655650$

$M(8) = \text{ASCII from 'A'} = 65$

$(M(8), z) = M(8)$  Combined with  $z$

$(M(8), z) = 65153196$

$e(8) = H(65153196)$

$e(8) = 50655754$

$M(9) = \text{ASCII from 'N'} = 78$

$(M(9), z) = M(9)$  Combined with  $z$

$(M(9), z) = 78153196$

$e(9) = H(78153196)$

$e(9) = 49665455$

$M(10) = \text{ASCII from ' ' } = 32$

$(M(10), z) = M(10)$  Combined with  $z$

$(M(10), z) = 32153196$

$e(10) = H(32153196)$

$e(10) = 57576753$

$M(11) = \text{ASCII from 'D'} = 68$

$(M(11), z) = M(11)$  Combined with  $z$

$(M(11), z) = 68153196$

$e(11) = H(68153196)$

$e(11) = 51656755$

$M(12) = \text{ASCII from 'T'} = 73$

$(M(12), z) = M(12)$  Combined with  $z$

$(M(12), z) = 73153196$

$e(12) = H(73153196)$

$e(12) = 66655650$

$M(13) = \text{ASCII from 'G'} = 71$

$(M(13), z) = M(13)$  Combined with  $z$

$(M(13), z) = 71153196$

$e(13) = H(71153196)$

$e(13) = 69575053$

$M(14) = \text{ASCII from 'T'} = 73$

$(M(14), z) = M(14)$  Combined with  $z$

$(M(14), z) = 73153196$

$e(14) = H(73153196)$

$e(14) = 66655650$

$M(15) = \text{ASCII from 'T'} = 84$

$(M(15), z) = M(15)$  Combined with  $z$

$(M(15), z) = 84153196$

$e(15) = H(84153196)$

$e(15) = 69545256$

$M(16) = \text{ASCII from 'A'} = 65$

$(M(16), z) = M(16)$  Combined with  $z$

$(M(16), z) = 65153196$

$e(16) = H(65153196)$

$e(16) = 50655754$

$M(17) = \text{ASCII from 'L'} = 76$

$(M(17), z) = M(17)$  Combined with  $z$

$(M(17), z) = 76153196$

$e(17) = H(76153196)$

$e(17) = 51677049$

3. Alice calculates the  $n$  value as follows:  $n = (r + se) \bmod q$

$n(1) = (r + (s \cdot e(1))) \bmod q$

$n(1) = (21 + (58 \cdot 65565550)) \bmod 59$

$n(1) = 50$

$n(2) = (r + (s \cdot e(2))) \bmod q$

$n(2) = (21 + (58 \cdot 67515350)) \bmod 59$

$n(2) = 23$



$$\begin{aligned}n(3) &= (r + (s \cdot e(3))) \bmod q \\n(3) &= (21 + (58 \cdot 49665455)) \bmod 59 \\n(3) &= 58\end{aligned}$$

$$\begin{aligned}n(4) &= (r + (s \cdot e(4))) \bmod q \\n(4) &= (21 + (58 \cdot 69575053)) \bmod 59 \\n(4) &= 10\end{aligned}$$

$$\begin{aligned}n(5) &= (r + (s \cdot e(5))) \bmod q \\n(5) &= (21 + (58 \cdot 51536752)) \bmod 59 \\n(5) &= 5\end{aligned}$$

$$\begin{aligned}n(6) &= (r + (s \cdot e(6))) \bmod q \\n(6) &= (21 + (58 \cdot 69545551)) \bmod 59 \\n(6) &= 12\end{aligned}$$

$$\begin{aligned}n(7) &= (r + (s \cdot e(7))) \bmod q \\n(7) &= (21 + (58 \cdot 66655650)) \bmod 59 \\n(7) &= 34\end{aligned}$$

$$\begin{aligned}n(8) &= (r + (s \cdot e(8))) \bmod q \\n(8) &= (21 + (58 \cdot 50655754)) \bmod 59 \\n(8) &= 15\end{aligned}$$

$$\begin{aligned}n(9) &= (r + (s \cdot e(9))) \bmod q \\n(9) &= (21 + (58 \cdot 49665455)) \bmod 59 \\n(9) &= 58\end{aligned}$$

$$\begin{aligned}n(10) &= (r + (s \cdot e(10))) \bmod q \\n(10) &= (21 + (58 \cdot 57576753)) \bmod 59 \\n(10) &= 11\end{aligned}$$

$$\begin{aligned}n(11) &= (r + (s \cdot e(11))) \bmod q \\n(11) &= (21 + (58 \cdot 51656755)) \bmod 59 \\n(11) &= 8\end{aligned}$$

$$\begin{aligned}n(12) &= (r + (s \cdot e(12))) \bmod q \\n(12) &= (21 + (58 \cdot 66655650)) \bmod 59 \\n(12) &= 34\end{aligned}$$

$$\begin{aligned}n(13) &= (r + (s \cdot e(13))) \bmod q \\n(13) &= (21 + (58 \cdot 69575053)) \bmod 59 \\n(13) &= 10\end{aligned}$$

$$\begin{aligned}n(14) &= (r + (s \cdot e(14))) \bmod q \\n(14) &= (21 + (58 \cdot 66655650)) \bmod 59 \\n(14) &= 34\end{aligned}$$

$$\begin{aligned}n(15) &= (r + (s \cdot e(15))) \bmod q \\n(15) &= (21 + (58 \cdot 69545256)) \bmod 59 \\n(15) &= 12\end{aligned}$$

$$\begin{aligned}n(16) &= (r + (s \cdot e(16))) \bmod q \\n(16) &= (21 + (58 \cdot 50655754)) \bmod 59 \\n(16) &= 15\end{aligned}$$

$$\begin{aligned}n(17) &= (r + (s \cdot e(17))) \bmod q \\n(17) &= (21 + (58 \cdot 51677049)) \bmod 59 \\n(17) &= 10\end{aligned}$$

Digital signatures generated as follows:

[65565550,50|67515350,23|49665455,58|69575053,10|51536752,5|69545551,12|66655650,34|50655754,15|49665455,58|57576753,11|51656755,8|66655650,34|69575053,10|66655650,34|69545256,12|50655754,15|51677049,10  
Digital signatures are e and n. Alice sends Bob a message and digital signature.

4. Bob did the following calculations:

$$z' = ((a^y) \cdot (v^e)) \bmod p$$

$$\begin{aligned}z'(1) &= ((a^y(1)) \bmod p \cdot (v^e(1)) \bmod p) \bmod p \\z'(1) &= (56937^{50} \bmod 166853) \cdot (56937^{65565550} \bmod 166853) \bmod 166853 \\z'(1) &= 153196\end{aligned}$$

$$\begin{aligned}z'(2) &= ((a^y(2)) \bmod p \cdot (v^e(2)) \bmod p) \bmod p \\z'(2) &= (56937^{23} \bmod 166853) \cdot (56937^{67515350} \bmod 166853) \bmod 166853 \\z'(2) &= 153196\end{aligned}$$

$$\begin{aligned}z'(3) &= ((a^y(3)) \bmod p \cdot (v^e(3)) \bmod p) \bmod p \\z'(3) &= (56937^{58} \bmod 166853) \cdot (56937^{49665455} \bmod 166853) \bmod 166853 \\z'(3) &= 153196\end{aligned}$$

$$\begin{aligned}z'(4) &= ((a^y(4)) \bmod p \cdot (v^e(4)) \bmod p) \bmod p \\z'(4) &= (56937^{10} \bmod 166853) \cdot (56937^{69575053} \bmod 166853) \bmod 166853 \\z'(4) &= 153196\end{aligned}$$

$$\begin{aligned}z'(5) &= ((a^y(5)) \bmod p \cdot (v^e(5)) \bmod p) \bmod p \\z'(5) &= (56937^5 \bmod 166853) \cdot (56937^{51536752} \bmod 166853) \bmod 166853 \\z'(5) &= 153196\end{aligned}$$

$$\begin{aligned}z'(6) &= ((a^y(6)) \bmod p \cdot (v^e(6)) \bmod p) \bmod p \\z'(6) &= (56937^{12} \bmod 166853) \cdot (56937^{69545551} \bmod 166853) \bmod 166853 \\z'(6) &= 153196\end{aligned}$$

$$\begin{aligned}z'(7) &= ((a^y(7)) \bmod p \cdot (v^e(7)) \bmod p) \bmod p \\z'(7) &= (56937^{34} \bmod 166853) \cdot (56937^{66655650} \bmod 166853) \bmod 166853 \\z'(7) &= 153196\end{aligned}$$

$$\begin{aligned}z'(8) &= ((a^y(8)) \bmod p \cdot (v^e(8)) \bmod p) \bmod p \\z'(8) &= (56937^{15} \bmod 166853) \cdot (56937^{50655754} \bmod 166853) \bmod 166853 \\z'(8) &= 153196\end{aligned}$$

$$\begin{aligned}z'(9) &= ((a^y(9)) \bmod p \cdot (v^e(9)) \bmod p) \bmod p \\z'(9) &= (56937^{58} \bmod 166853) \cdot (56937^{58} \bmod 166853) \bmod 166853\end{aligned}$$



$(56937^{49665455} \bmod 166853)$   
 $\bmod 166853$   
 $z'(9) = 153196$   
 $z'(10) = ((a^y(10)) \bmod p \cdot (v^e(10)) \bmod p) \bmod p$   
 $z'(10) = (56937^{11} \bmod 166853) \cdot$   
 $(56937^{57576753} \bmod 166853)$   
 $\bmod 166853$   
 $x'(10) = 153196$   
 $z'(11) = ((a^y(11)) \bmod p \cdot (v^e(11)) \bmod p) \bmod p$   
 $z'(11) = (56937^8 \bmod 166853) \cdot$   
 $(56937^{51656755} \bmod 166853)$   
 $\bmod 166853$   
 $x'(11) = 153196$   
 $z'(12) = ((a^y(12)) \bmod p \cdot (v^e(12)) \bmod p) \bmod p$   
 $z'(12) = (56937^{34} \bmod 166853) \cdot$   
 $(56937^{66655650} \bmod 166853)$   
 $\bmod 166853$   
 $z'(12) = 153196$   
 $z'(13) = ((a^y(13)) \bmod p \cdot (v^e(13)) \bmod p) \bmod p$   
 $z'(13) = (56937^{10} \bmod 166853) \cdot$   
 $(56937^{69575053} \bmod 166853)$   
 $\bmod 166853$   
 $z'(13) = 153196$   
 $z'(14) = ((a^y(14)) \bmod p \cdot (v^e(14)) \bmod p) \bmod p$   
 $z'(14) = (56937^{34} \bmod 166853) \cdot$   
 $(56937^{66655650} \bmod 166853)$   
 $\bmod 166853$   
 $z'(14) = 153196$   
 $z'(15) = ((a^y(15)) \bmod p \cdot (v^e(15)) \bmod p) \bmod p$   
 $z'(15) = (56937^{12} \bmod 166853) \cdot$   
 $(56937^{69545256} \bmod 166853)$   
 $\bmod 166853$   
 $z'(15) = 153196$   
 $z'(16) = ((a^y(16)) \bmod p \cdot (v^e(16)) \bmod p) \bmod p$   
 $z'(16) = (56937^{15} \bmod 166853) \cdot$   
 $(56937^{50655754} \bmod 166853)$   
 $\bmod 166853$   
 $z'(16) = 153196$   
 $z'(17) = ((a^y(17)) \bmod p \cdot (v^e(17)) \bmod p) \bmod p$   
 $z'(17) = (56937^{10} \bmod 166853) \cdot$   
 $(56937^{51677049} \bmod 166853)$   
 $\bmod 166853$   
 $z'(17) = 153196$

5. Bob combines M and z' and performs verification:  $e = H(M, z')$

$M(1) = \text{ASCII from 'P'} = 80$   
 $(M(1), z'(1)) = M(1) \text{ combined with } z'(1)$   
 $(M(1), z'(1)) = 80153196$   
 $e(1) = H(80153196)$   
 $65565550 = 65565550 \text{ (TRUE)}$   
 $M(2) = \text{ASCII from 'E'} = 69$

$(M(2), z'(2)) = M(2) \text{ combined with } z'(2)$   
 $(M(2), z'(2)) = 69153196$   
 $e(2) = H(69153196)$   
 $67515350 = 67515350 \text{ (TRUE)}$

$M(3) = \text{ASCII from 'N'} = 78$   
 $(M(3), z'(3)) = M(3) \text{ combined with } z'(3)$   
 $(M(3), z'(3)) = 78153196$   
 $e(3) = H(78153196)$   
 $49665455 = 49665455 \text{ (TRUE)}$

$M(4) = \text{ASCII from 'G'} = 71$   
 $(M(4), z'(4)) = M(4) \text{ combined with } z'(4)$   
 $(M(4), z'(4)) = 71153196$   
 $e(4) = H(71153196)$   
 $69575053 = 69575053 \text{ (TRUE)}$

$M(5) = \text{ASCII from 'U'} = 85$   
 $(M(5), z'(5)) = M(5) \text{ combined with } z'(5)$   
 $(M(5), z'(5)) = 85153196$   
 $e(5) = H(85153196)$   
 $51536752 = 51536752 \text{ (TRUE)}$

$M(6) = \text{ASCII from 'J'} = 74$   
 $(M(6), z'(6)) = M(6) \text{ combined with } z'(6)$   
 $(M(6), z'(6)) = 74153196$   
 $e(6) = H(74153196)$   
 $69545551 = 69545551 \text{ (TRUE)}$

$M(7) = \text{ASCII from 'T'} = 73$   
 $(M(7), z'(7)) = M(7) \text{ combined with } z'(7)$   
 $(M(7), z'(7)) = 73153196$   
 $e(7) = H(73153196)$   
 $66655650 = 66655650 \text{ (TRUE)}$

$M(8) = \text{ASCII from 'A'} = 65$   
 $(M(8), z'(8)) = M(8) \text{ combined with } z'(8)$   
 $(M(8), z'(8)) = 65153196$   
 $e(8) = H(65153196)$   
 $50655754 = 50655754 \text{ (TRUE)}$

$M(9) = \text{ASCII from 'N'} = 78$   
 $(M(9), z'(9)) = M(9) \text{ combined with } z'(9)$   
 $(M(9), z'(9)) = 78153196$   
 $e(9) = H(78153196)$   
 $49665455 = 49665455 \text{ (TRUE)}$

$M(10) = \text{ASCII from ' '} = 32$   
 $(M(10), z'(10)) = M(10) \text{ combined with } z'(10)$   
 $(M(10), z'(10)) = 32153196$   
 $e(10) = H(32153196)$   
 $57576753 = 57576753 \text{ (TRUE)}$

$M(11) = \text{ASCII from 'D'} = 68$   
 $(M(11), z'(11)) = M(11) \text{ combined with } z'(11)$   
 $(M(11), z'(11)) = 68153196$   
 $e(11) = H(68153196)$   
 $51656755 = 51656755 \text{ (TRUE)}$

$M(12) = \text{ASCII from 'I'} = 73$



$(M(12), z'(12)) = M(12)$  combined with  $z'(12)$   
 $(M(12), z'(12)) = 73153196$   
 $e(12) = H(73153196)$   
 $66655650 = 66655650$  (TRUE)

$M(13) = \text{ASCII from 'G'} = 71$   
 $(M(13), z'(13)) = M(13)$  combined with  $z'(13)$   
 $(M(13), z'(13)) = 71153196$   
 $e(13) = H(71153196)$   
 $69575053 = 69575053$  (TRUE)

$M(14) = \text{ASCII from 'T'} = 73$   
 $(M(14), z'(14)) = M(14)$  combined with  $z'(14)$   
 $(M(14), z'(14)) = 73153196$   
 $e(14) = H(73153196)$   
 $66655650 = 66655650$  (TRUE)

$M(15) = \text{ASCII from 'T'} = 84$   
 $(M(15), z'(15)) = M(15)$  combined with  $z'(15)$   
 $(M(15), z'(15)) = 84153196$   
 $e(15) = H(84153196)$   
 $69545256 = 69545256$  (TRUE)

$M(16) = \text{ASCII from 'A'} = 65$   
 $(M(16), z'(16)) = M(16)$  combined with  $z'(16)$   
 $(M(16), z'(16)) = 65153196$   
 $e(16) = H(65153196)$   
 $50655754 = 50655754$  (TRUE)

$M(17) = \text{ASCII from 'L'} = 76$   
 $(M(17), z'(17)) = M(17)$  combined with  $z'(17)$   
 $(M(17), z'(17)) = 76153196$   
 $e(17) = H(76153196)$   
 $51677049 = 51677049$  (TRUE)

The result of the operation  $H(M, z')$  is equal to the value  $e$  so that the digital signature verification process succeeds.

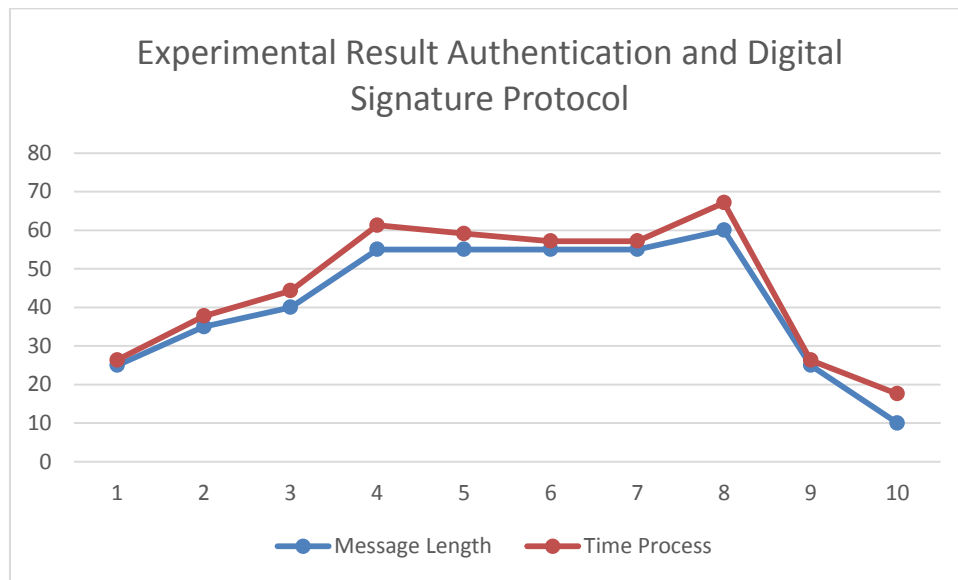
The following is the process of experimenting the delivery of messages with different message lengths in the network as well as the amount of time required for the authentication process.

**Table-1.** Experimental result.

No.	p, q, a Key	Length message	Time process
1	p=427249 q=43 a=58978	25	1.35 ms
2	p=427249 q=43 a=58978	35	2.765 ms
3	p=9895759 q=641 a=54251	40	4.31 ms
4	p=704461 q=59 a=34253	55	6.292 ms
5	p=490201 q=43 a=20191	55	4.13 ms
6	p=1740527 q=419 a=38820	55	2.19 ms
7	p=145361 q=23 a=70968	55	2.16 ms
8	p=582449 q=23 a=82637	60	7.13 ms
9	p=207763 q=31 a=58336	25	1.31 ms
10	p=799789 q=73 a=65266	65	7.61 ms

Based on experimental results conducted in Table-1 found that the process time of the use of protocols depends on the value of  $p$  and  $a$  as prime numbers, from the table above generated graphs of process time as in Figure-1 below:





**Figure-1.** Experimental result authentication and signature protocol.

Figure-1 shows that the time it takes to secure a message depends on the value of  $p$  and  $a$ , the greater value of  $p$  and  $a$ , the longer it takes time to process.

## CONCLUSIONS

After completing the experiment of Schnorr Authentication and Digital Signature Scheme, the authors draw the conclusion that the use of the Schnorr scheme can serve as a additional security mechanism especially in two-way communication process and the process is also not complicated if implemented, one of the weaknesses that may occur is to take time much longer than cryptography process, and for next research this weakness could be solved.

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