



OPTIMAL OPERATION OF RENEWABLE ENERGY IRRIGATION SYSTEM USING PARTICLE SWARM OPTIMIZATION

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ABSTRACT

In rural areas which are located far from the electrical grid, renewable energy systems such as photovoltaic (PV) energy are investigated. The most popular PV application is solar water pumping for irrigation. DC-DC converter and maximum power point tracking are used because the PV modules output varies widely due to varying weather conditions. The water pump is driven by a three phase induction motor through a voltage source inverter (VSI). However, the control of induction motor is known to be difficult because it's highly non-linear and time variant. One method to mitigate this is by using vector control techniques to control the VSI as they offer a number of benefits including speed control and regulation over a wide range and fast dynamic response. The proportional - integral (PI) controller is most commonly used in the speed control loop of vector control. This paper deals with the design of the speed PI controller parameters (gains) using particle swarm optimization (PSO) technique and compares it with the conventional Ziegler-Nichols (ZN) method. Different objective functions have been proposed which are used to evaluate the optimization algorithm. The optimum solution mainly converges to a minimum error which affects the control parameters such as the maximum overshoot, rise time and settling time of the system. Simulation results are obtained using Matlab/Simulink program for photovoltaic pump application during load variation (pump head and flow rate variation). The results show the advantage of the PSO-based optimization approach.

Keywords: indirect field oriented control, objective function, particle swarm optimization, photovoltaic pump, PI controller.

1. INTRODUCTION

Solar power generation is continuously increasing in many power systems around the world in an effort to increase renewable energy penetration as it offers an excellent solution for providing sustainable and clean energy. The most common PV application is solar water pumping (Chandel *et al.*, 2015; Moubarak *et al.*, 2017). The dc output voltage of PV arrays is connected to a dc/dc converter using a maximum power point tracking (MPPT) controller to maximize their produced energy (De Brito *et al.*, 2013; Forouzesh *et al.*, 2017). Then, that converter is linked to a dc/ac voltage source inverter (VSI) to let the PV system push electric power to the ac utility or to feed ac loads (Wu, 2006). Indirect field oriented control (IFOC) technique is used to control the VSI fed three phase induction motor drive system as it provides an excellent performance in terms of static and dynamic speed regulation and rapid response to transients (Wu, 2006; Moubarak *et al.*, 2018). The Proportional – Integral (PI) controller in the IFOC speed control loop is used to calculate the torque reference by comparing the speed reference with the measured rotor speed. Tuning of the PI controller gains is very important because they have great effect on the control system performance and stability. Over the years, several PI tuning methods have been proposed. Conventional methods include Ziegler-Nichols, Cohen-Coon, Astrom & Hagglund and many others (Pedret *et al.*, 2002). However, these conventional techniques don't provide good tuning and often result in a high overshoot, long settling time and slow transient response. To overcome these drawbacks, several artificial intelligence and random search techniques such as neural networks, fuzzy systems, genetic algorithm, simulated annealing, particle swarm optimization, etc., have been

employed (Gaing, 2004). In this paper, the particle swarm optimization technique (PSO) is used due to its simplicity and ease of implementation, and it can generate a high quality solution within shorter calculation time and stable convergence characteristics than the others (Liang *et al.*, 2006). Particle swarm optimization technique is a modern algorithm that has been developed from the behavior of organisms such as fish schooling and bird flocking. The technique conducts search using a population of particles. Every particle updates its velocity and position in accordance to its own experience and other particles' experiences. Each particle's position represents a candidate solution to the problem thus has more efficiency for finding the optimal solution (Kennedy and Eberhart, 1995; Shi and Eberhart, 1998). The convergence of the PSO algorithm toward the global optimal solution is guided by the objective function. The most commonly used functions are the time domain integral error performance criteria (Chin *et al.*, 2004), but these criteria have their own advantages and disadvantages. These drawbacks were overcome with a performance criterion in which the unit step time parameters are used with a single weighting factor (Gaing, 2004).

This paper is organized into sections as follows: Section 2 gives an overview of the proposed system. Section 3 presents the indirect field oriented control of an induction motor. The conventional Ziegler-Nichols (ZN) method is described in section 4. Section 5 presents the particle swarm optimization (PSO) method. Multiple performance assessment criteria are presented in section 6. Section 7 shows the simulation results and compares the speed response due to tuning using ZN and

PSO with various assessment criteria. Furthermore, the PV pump performance is observed over



various weather and loading conditions. Section 8 concludes the paper with merits of the proposed system.

2. OVERVIEW OF THE PROPOSED SYSTEM

The proposed photovoltaic water pumping system is shown in Figure-1, and it has the following elements:

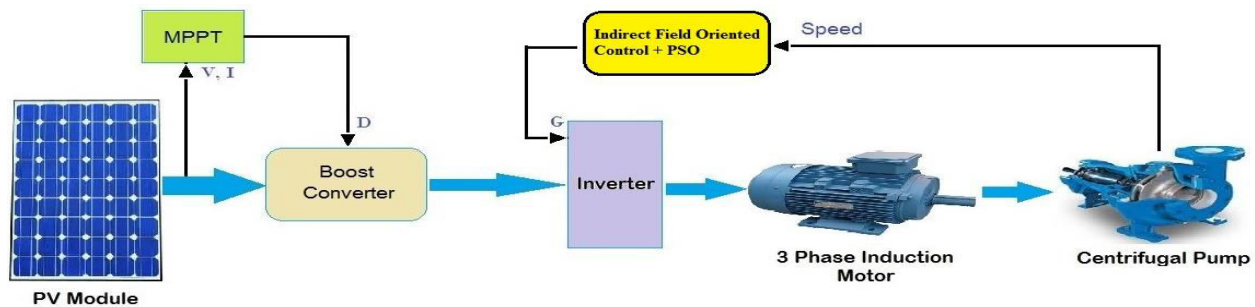


Figure-1. Proposed PSO optimized photovoltaic water pumping system.

- PV Array that converts the solar irradiation into DC power. The PV array used consists of 5 Series-connected modules per string and 5 Parallel strings in order to meet the load needs. AXN-P6T170 PV module manufactured by Auxin solar (Auxin Solar INC) is taken as the reference module for simulation and it has the following electrical specifications as shown in Table-1.

Table-1. Electrical characteristics data of PV module taken from the datasheet.

Parameter	Value
Maximum Power	169.932 W
Open Circuit Voltage (Voc)	28.8 V
Voltage at Maximum Power Point (Vmpp)	23.8 V
Temperature Coefficient of Voc (β)	- 0.37 (% / °C)
Cells / Module	48
Short Circuit Current (Isc)	7.72 A
Current at Maximum Power Point (Impp)	7.14 A
Temperature Coefficient of Isc (α)	0.111 (% / °C)

- Boost DC-DC Converter which boosts up the PV voltage to the predetermined levels. The boost converter parameters shown in Table-2 were calculated using the equations given in (Mohan *et al.*, 2003).

Table-2. Boost converter and input filter parameters.

Parameter	Value
Inductor (L)	$4.73e^{-3}$ H
Capacitor (C)	$2.26e^{-4}$ F
Input Filter Capacitor (Cin)	$1.9 e^{-3}$ F

- Maximum Power Point Tracking (MPPT) that tracks the PV optimized operation point for power extraction

by controlling the boost converter duty cycle. The MPPT technique used in this paper is the perturb and observe (P&O) method (De Brito *et al.*, 2013).

- VSI that converts the DC power to AC power.
- Motor Control Unit that controls the speed and torque of the induction motor using indirect field oriented control which in turn controls the pump performance. Also, the particle swarm optimization algorithm is employed.
- Motor-Pump set which is a three phase induction motor driving a centrifugal pump of type (LKH-/ LKHP-/ LKHI-60, 50 Hz) manufactured by Alfa Laval (Alfa Laval Corporate AB). The motor parameters (Moubarak *et al.*, 2017) are given in Table-3.

Table-3. Three phase induction motor parameters.

Parameter	Value
Rated Power	4 Kw
Rated Line to Line Voltage	400 V
Rated Frequency	50 Hz
Number of Poles	4
Stator Resistance	1.47 Ω
Stator Leakage Reactance	1.834 Ω
Rotor Resistance	1.393 Ω
Rotor Leakage Reactance	1.834 Ω
Magnetizing Reactance	54.1 Ω
Moment of Inertia	0.012 Kg.m ²
Rated Speed	1425 RPM
Rated Torque	26.8 N.m
Efficiency	86.6%

3. INDIRECT FIELD ORIENTED CONTROL

Field oriented control principles applied to an induction motor are based on the decoupling between the current components used for generating magnetizing flux



and torque (Wu, 2006). This is done by performing the transformation from three phase (abc) to d-q rotating reference frame using Clarke and Park transformations. This allows the induction motor to be controlled as a simple DC motor. The field oriented control utilizes the stator current components as control variables. The d-component of the stator current acts on the rotor flux, whereas the q-component is proportional to the motor torque as the control of the motor flux is obtained indirectly by controlling the motor currents. Considering the d-q model of the induction machine in the reference

frame rotating at synchronous speed ω_e . The i_{ds} component of the stator current would be aligned with the rotor field, and the i_{qs} component would be perpendicular to i_{ds} .

In indirect field oriented control (IFOC), the rotor flux angle θ_f is obtained from detected rotor position angle θ_r and calculated slip angle θ_{sl} . A typical block diagram of the IFOC with current controlled VSI is shown in Figure-2.

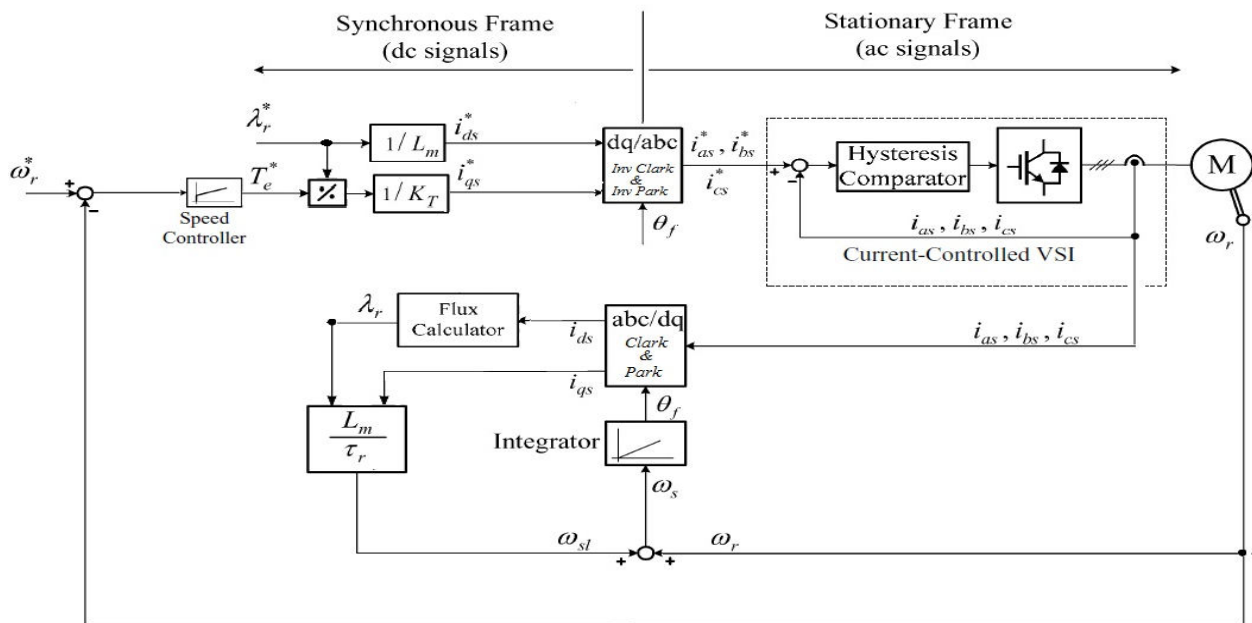


Figure-2. IFOC with a current regulated VSI.

Since the rotor speed ω_r is directly measured, the rotor flux angle θ_f can be found from:

$$\theta_f = \int (\omega_r + \omega_{sl}) dt \quad (1)$$

The angular slip speed ($\omega_{sl} = \omega_e - \omega_r$) can be derived from the motor synchronous reference frame model.

$$\frac{d}{dt} \lambda_r = -R_r i_r - j\omega_{sl} \lambda_r \quad (2)$$

Where i_s & i_r are the stator and rotor currents, respectively; R_r is the rotor winding resistance; λ_r is the rotor flux; L_r & L_{lr} are the rotor self and leakage inductances, respectively; L_m is the magnetizing inductance; and P is the number of poles. From the rotor current:

$$i_r = \frac{1}{L_r} (\lambda_r - L_m i_s) \quad (3)$$

$$L_r = L_{lr} + L_m \quad (4)$$

$$\frac{d}{dt} \lambda_r = -\frac{R_r}{L_r} (\lambda_r - L_m i_s) - j\omega_{sl} \lambda_r \quad (5)$$

$$\lambda_r + \tau_r \left(\frac{d}{dt} \lambda_r + j\omega_{sl} \lambda_r \right) = L_m i_s \quad (6)$$

Where τ_r is the rotor time constant, and equals:

$$\tau_r = \frac{L_r}{R_r} \quad (7)$$

Dividing Equation (6) into the d-q axis components and taking into account the rotor flux orientation ($j\lambda_{qr} = 0$ & $\lambda_{dr} = \lambda_r$):

$$\lambda_r + \tau_r \left(\frac{d}{dt} \lambda_r \right) = L_m i_{ds} \quad (8)$$

$$\omega_{sl} \lambda_r \tau_r = L_m i_{qs} \quad (9)$$

$$\text{So } \omega_{sl} = \frac{L_m i_{qs}}{\lambda_r \tau_r} \quad (10)$$

From Equation (8) and since the rotor reference flux λ_r^* is normally kept constant during operation ($\frac{d}{dt} \lambda_r^* = 0$):



$$i_{ds}^* = \frac{\lambda_r^*}{L_m} \quad (11)$$

The q-axis current reference i_{qs}^* can be obtained from the electromagnetic torque equation:

$$T_e = \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} (i_{qs} \lambda_{dr} - i_{ds} \lambda_{qr}) \quad (12)$$

Taking into account the rotor flux orientation:

$$i_{qs}^* = \frac{T_e^*}{K_T \lambda_r^*} \quad (13)$$

$$\text{Where } K_T = \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} \quad (14)$$

$$\text{Let } C = K_T \lambda_r^*, \text{ so } i_{qs}^* = \frac{T_e^*}{C} \quad (15)$$

Where T_e^* is the reference electromagnetic torque.

Speed controller

The speed PI block is an ordinary PI regulator with the speed error signal calculated from the comparison of the speed reference value (ω_r^*) and the actual speed (ω_r) as its input. The torque reference value is its output which is then provided to the IFOC block as input. And the mechanical system equation:

$$T_e = T_L + J \frac{d\omega_r}{dt} + f \omega_r \quad (16)$$

The block diagram of speed control loop can be seen in Figure-3.

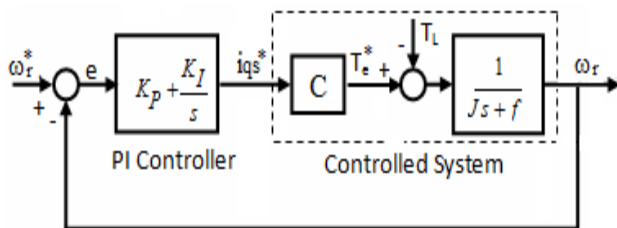


Figure-3. Block diagram of speed control loop.

If $T_L=0$, the closed loop transfer function is as follows:

$$\frac{\omega_r}{\omega_r^*} = \frac{(K_p s + K_i) C}{J s^2 + (K_p C + f) s + K_i C} \quad (17)$$

where J is the moment of inertia and f is the friction coefficient.

4. TUNING OF PI USING ZIEGLER-NICHOLS METHOD

The Ziegler-Nichols (ZN) tuning used here is based on the open-loop step response of the system as shown in Figure-4. This type of response is typical of a first order system with transportation delay. The response is characterized by two parameters, L the delay time and T

the time constant. These are found by drawing a tangent to the step response at its point of inflection and noting its intersections with the time axis and the steady state value. These parameters are used to determine the controller's gains (Hang *et al.*, 1991) as shown in Table-4.

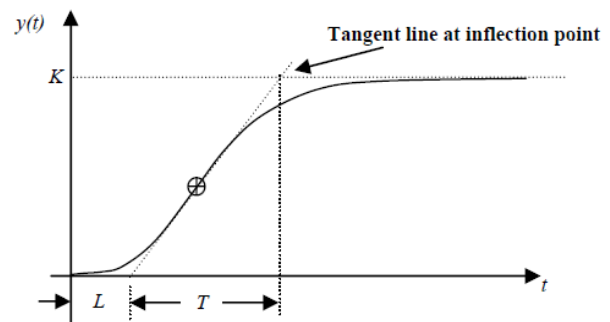


Figure-4. Response curve for Ziegler-Nichols method.

Table-4. Ziegler-Nichols open-loop tuning parameters.

Controller	K_p	$T_i = K_p/K_i$	$T_d = K_d/K_p$
PI	0.9 (T/L)	L/0.3	0

Where T_i is the reset time, and T_d is the derivative time.

5. TUNING OF PI USING PARTICLE SWARM OPTIMIZATION

The particle swarm optimization (PSO) can be defined as an optimization technique based on evolutionary computation. It was developed through the simulation of simplified social systems, and has been found to be robust in solving continuous nonlinear optimization problems. PSO is a population based stochastic optimization technique where individuals, referred to as particles, are grouped into a swarm. Every particle in the swarm represents a candidate solution to the optimization problem. Each particle is flown through a multidimensional search space, adjusting its position in search space according to its own experience and that of neighbouring particles. Therefore, a particle makes use of best position encountered by itself and that of its neighbours to position itself towards an optimal solution. The effect is that particles fly toward a minimum, while still searching a wide area around the best solution. The performance of each particle is measured using a predefined objective (fitness) function, which encapsulate the characteristics of the optimization problem (Kennedy and Eberhart, 1995; Shi and Eberhart, 1998).

Each particle is treated as a point in a j -dimensional space. The i th particle is represented as $X_i = (x_{i1}, x_{i2}, \dots, x_{ij})$. The best previous position (giving the minimum fitness value) of any particle is recorded and represented as $P_i = (p_{i1}, p_{i2}, \dots, p_{ij})$, this is called pbest. The index of the best particle among all particles in the population is represented by the symbol g , called as gbest. The velocity for the particle i is represented as $V_i =$



$(v_{i1}, v_{i2}, \dots, v_{ij})$. The particles are updated according to the following equations:

$$V_{ij}^{n+1} = w * V_{ij}^n + r_1 c_1 (P_{ij}^n - X_{ij}^n) + r_2 c_2 (P_{gj}^n - X_{ij}^n) \quad (18)$$

$$X_{ij}^{n+1} = X_{ij}^n + V_{ij}^{n+1} \quad (19)$$

where w is the inertia weight, c_1 and c_2 are acceleration coefficients, r_1 and r_2 are random numbers uniformly distributed between 0 and 1, and n represents the iteration number.

Equation (18) is used to calculate particle's new velocity according to its previous velocity and the distances of its current position from its own best experience (position) and the group's best experience. Then the particle flies toward a new position according to Equation (19). The performance of each particle is measured according to a pre-defined objective function (performance index), which is related to the problem to be solved. c_1 and c_2 represent the weighting of the stochastic acceleration terms that pull each particle toward p_{best} and g_{best} positions. Low values, allow particles to roam far from the target regions before being tugged back. On the other hand, high values result in abrupt movement toward, or past, target regions. Hence, the acceleration constants c_1 and c_2 were set to be 2.0 according to past experiences. Suitable selection of inertia weight w provides a balance between global and local explorations, thus requiring less iteration on average to find a sufficiently optimal solution. As originally developed, w often decreases linearly from about $w_{max} = 0.9$ to $w_{min} = 0.4$ during a run. In general, the inertia weight w is set according to the following equation:

$$w = w_{max} - \frac{w_{max} - w_{min}}{iter_{max}} \times iter \quad (20)$$

Where $iter_{max}$ is the maximum number of iterations (generations), and $iter$ is the current number of iterations.

The computational flowchart for the proposed PSO is shown in Figure-5.

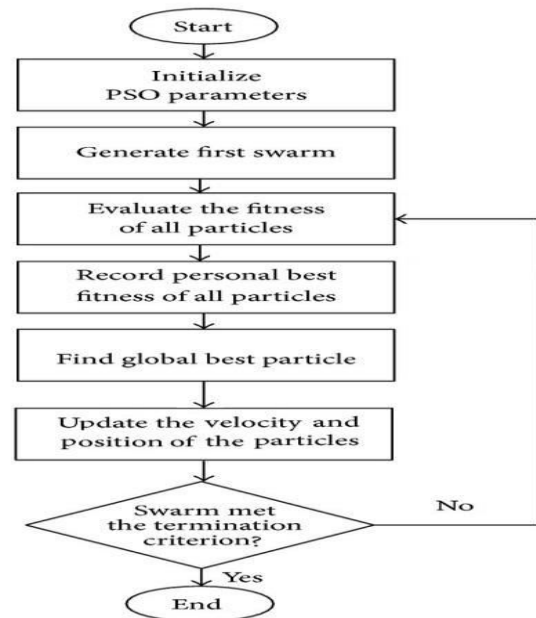


Figure-5. Flowchart of particle swarm optimization.

The termination criterion used here is when the maximum number of iterations is reached which is 100 iteration. Considering that there are 50 individuals (particles) in the population. Since there are two parameters (K_p & K_i) to control, position and velocity are represented by matrices with the dimension of 2×50 by using Equations (18) and (19). The values of (K_p & K_i) are assumed to be from 0 to 50. The position represents the PI controller gains (K_p & K_i).

6. EVALUATION OF THE OBJECTIVE FUNCTION

The performance of the control system is usually evaluated based on its transient response behavior. To design an efficient controller, the objective is to improve the system response by minimizing the error between the input signal $u(t)$ and the output $y(t)$. In general, the error signal is expressed as:

$$e(t) = u(t) - y(t) \quad (21)$$

The error signal defined by Equation (21) is widely used in the integral performance criteria in the frequency domain (Chin *et al.*, 2004) such as the integral square error (ISE), integral absolute error (IAE), integral time square error (ITSE), and the integral time absolute error (ITAE). The ISE and IAE weigh all errors equally and independent of time. Consequently, optimizing the control system response can result in a response with relatively small overshoot but long settling time or vice versa. To overcome this problem the ITSE and ITAE criteria weigh the error such that late error values are considerably taken into account. The ITSE and ITAE performance criteria formulas are as follows:

$$ITSE = \int_0^{\infty} t e^2(t) dt \quad (22)$$

$$\text{ITAE} = \int_0^{\infty} t |e(t)| dt \quad (23)$$

However, ITSE and ITAE can result in a multiple minimum optimization problem. In addition, all the integral performance criteria attempt to minimize only the error which does not necessarily mean minimizing all the basic evaluation parameters such as the maximum overshoot (M_p), rise time (t_r), settling time (t_s), and the steady-state error (E_{ss}). A performance criterion in the time domain where the aforementioned parameters are evaluated and minimized was proposed (Gaing, 2004) as shown in Equation (24).

$$\text{Fun} = (1 - e^{-\beta}) \cdot (M_p + E_{ss}) + e^{-\beta} \cdot (t_s - t_r) \quad (24)$$

Where β is the weighting factor. β can be set greater than 0.7 to reduce the overshoot and steady-state error or less than 0.7 to reduce the rise time and settling time. For this system, it has been found that setting β to 1.5 yields the best result.

Therefore, for tuning a PI controller based on the PSO technique, the performance evaluation indices ITSE, ITAE, and Fun will be used as the objective function and their responses will be compared with each other in order to find the optimal set of the PI controller gains. The structure of the PSO tuned IFOC speed PI controller with

its performance evaluated using the objective function is shown in Figure-6.

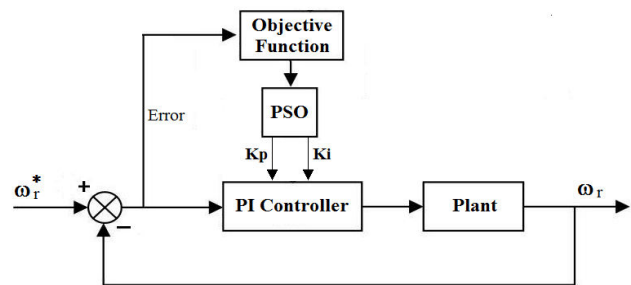


Figure-6. Implementation of PSO algorithm for tuning the PI controller.

7. RESULTS AND SIMULATION

This section shows the simulation results using Matlab/Simulink software for the system with the PI controller tuned using Ziegler-Nichols and PSO methods. Furthermore, the results obtained using different performance evaluation indices for the PSO tuned PI controller are shown and compared. Finally, the system is observed for a variable speed PV water pump over a variety of weather and loading conditions. Figure-7 shows the Matlab/Simulink implementation of the proposed variable speed PV pump.

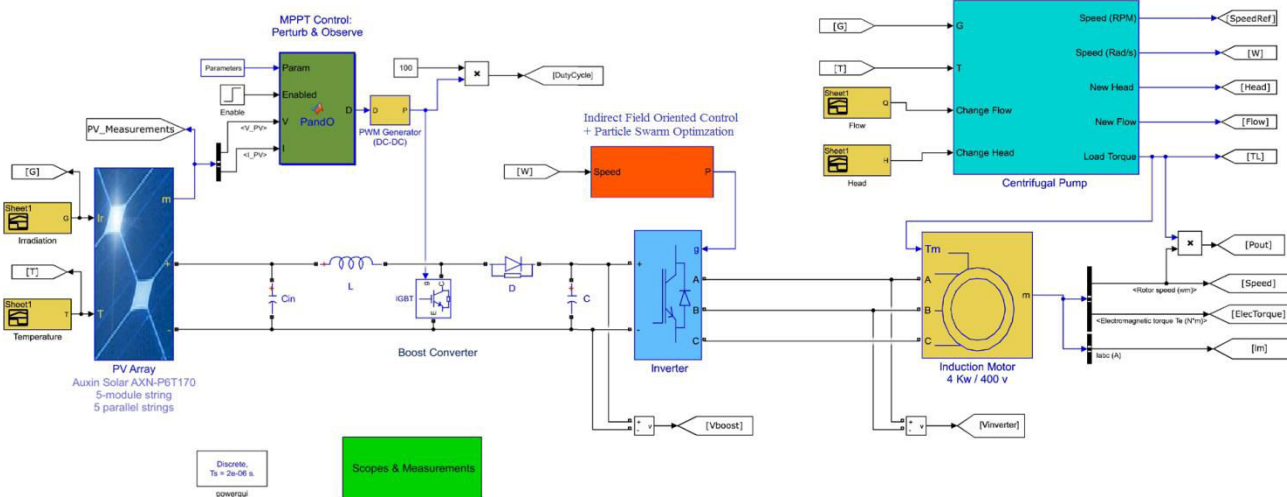


Figure-7. Matlab/Simulink model for the proposed system.

Figure-8 shows the motor speed response at its rated speed of 1425 rpm for the PI controller gains (K_p & K_i) obtained using Ziegler-Nichols (ZN) method and the

gains obtained using PSO with ITSE, ITAE and Fun performance assessment indices as indicated in Table-5.

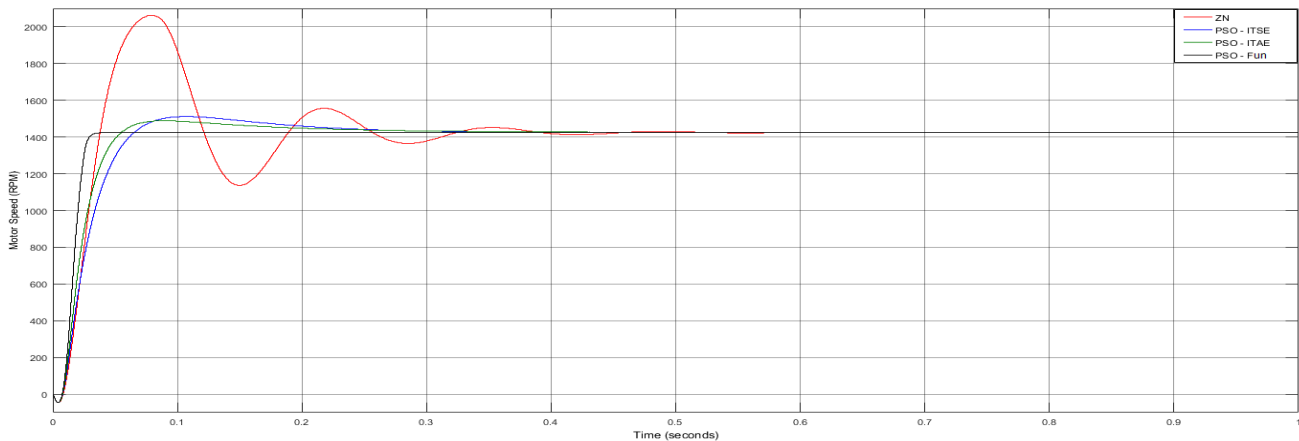


Figure-8. Motor speed curves for different PI controller gains.

Table-5. The optimized parameters of PI controller.

Tuning Method	K_p	K_i
ZN	0.31	30
PSO - ITSE	0.65	6.97
PSO - ITAE	0.9	7.88
PSO - Fun	5.1	8.03

Comparative results for the speed response performance in the time domain shown in Figure-8 are evaluated based on the rise time (t_r), the settling time (t_s), the maximum overshoot (M_p), and the peak time (t_p) as presented in Table-6.

Table-6. Comparison of time domain specifications.

Tuning Method	t_r (s)	t_s (s)	M_p (%)	t_p (s)
ZN	0.026	0.31	44.77	0.078
PSO - ITSE	0.045	0.2117	6.1	0.107
PSO - ITAE	0.036	0.178	4.47	0.09
PSO - Fun	0.017	0.029	0.0038	0.04

It is clear from the responses that the PSO based controller has greatly reduced the overshoot and the settling time compared to the Ziegler-Nichols tuned controller.

Furthermore, the PI controller tuned using the PSO evaluated using with the Fun assessment criterion (PSO - Fun) gives the best response as it reduces the overshoot to almost zero and has the fastest rise, settling and peak times.

The PSO global best (Best Cost) solution is selected for the particle which has the smallest value based on the Fun performance assessment criterion for the 100 iterations as shown in Figure-9.

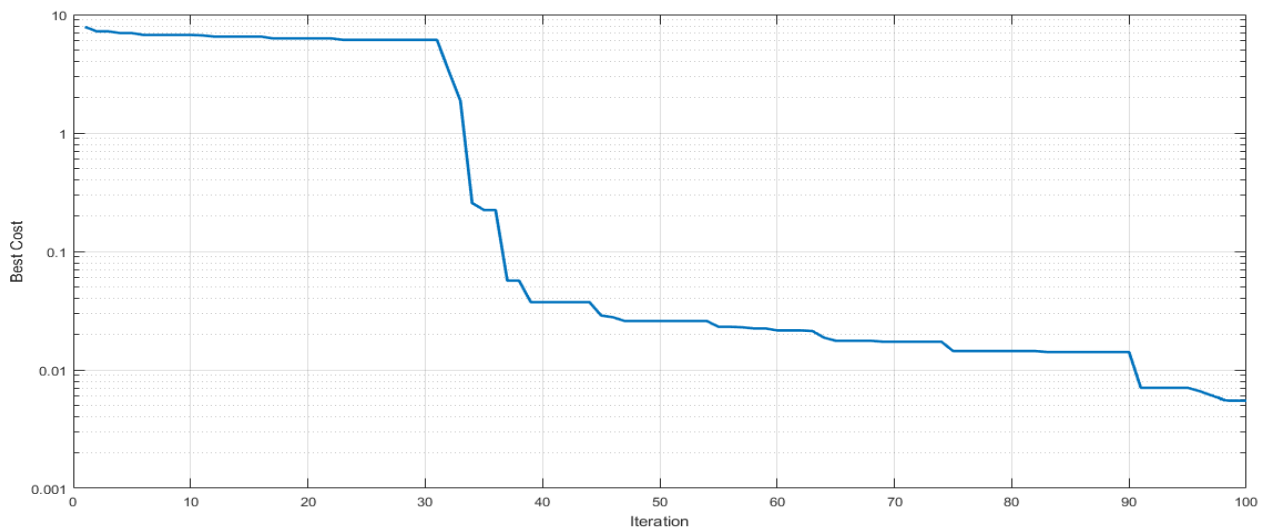


Figure-9. PSO-Fun global best value throughout the 100 iterations.

It can be seen that global best value is minimized throughout the iterations, and thus, the solution is optimized. The PI controller gains obtained using PSO with its objective function evaluated using the Fun equation (PSO - Fun) is used to simulate the variable speed PV pump model. ($K_p = 5.1$ & $K_i = 8.03$).

7.1 Variable speed PV pump

The PV module output changes with the variation of the weather conditions (solar irradiation and

temperature). Furthermore, the PV pump proposed varies its speed to accommodate for the variation of the hydraulic requirements (flow rate and pumping head). This is done by employing the pump Affinity laws (Igor *et al.*, 2008). Table-7 shows the required pump motor speed due to the variation of the weather conditions (solar irradiation (G) and temperature (T)) and the variation of hydraulic requirements of the pump (flow rate (Q) and pumping head (H)) along the simulation time.

Table-7. Pump motor speed due to the variation of solar irradiation (G), temperature (T), pump flow rate (Q) and head (H).

Time	G (w/m ²)	T (°C)	Q (m ³ /h)	H (m)	Motor speed (RPM)
0-0.3	1000	25	67	12.47	1425
0.3-0.4	900	25	67	11.17	1363
0.4-0.5	900	35	106	5.097	1274
0.5-0.6	1000	35	106	6.203	1326
0.6-0.7	1000	25	67	12.47	1425

Figure-10 shows the variation of the solar irradiation and temperature and the pump flow rate and head along the simulation time as in Table-7.

Figure-11 shows the pump reference (required) motor speed due to the variation of the weather and

loading conditions as illustrated in Table-7 versus the actual (measured) motor speed. As can be seen, the motor follows its required reference speed with an accurate and fast response which shows the merits of the proposed technique.

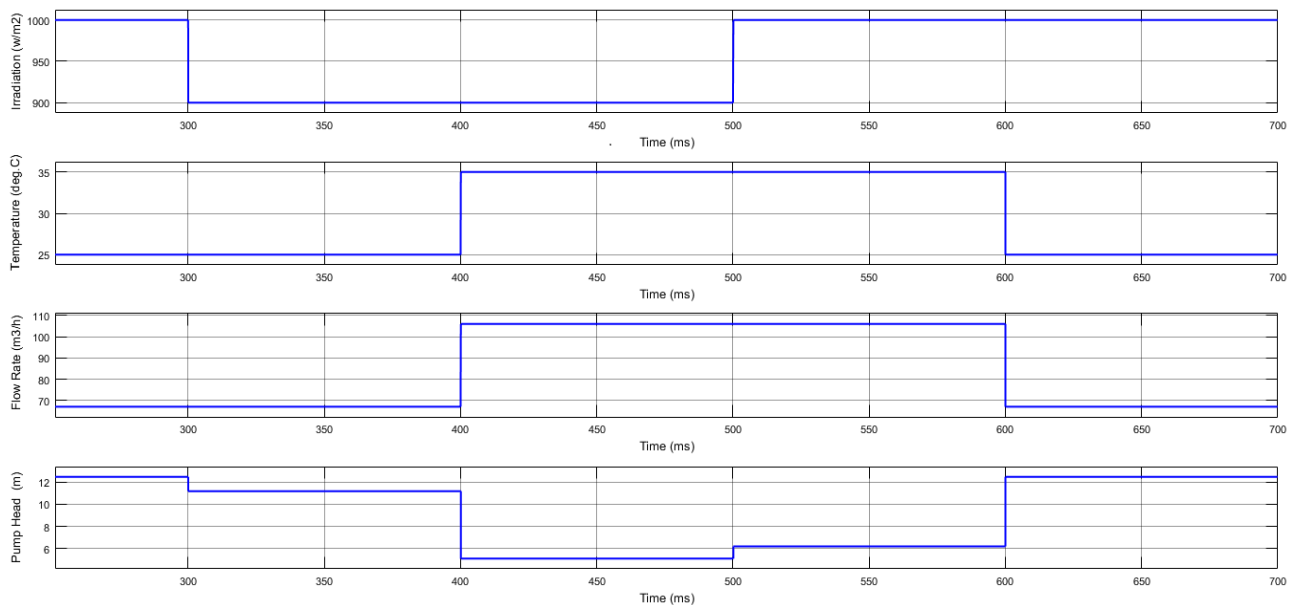


Figure-10. Solar irradiation, temperature, pump flow rate, and head variation.

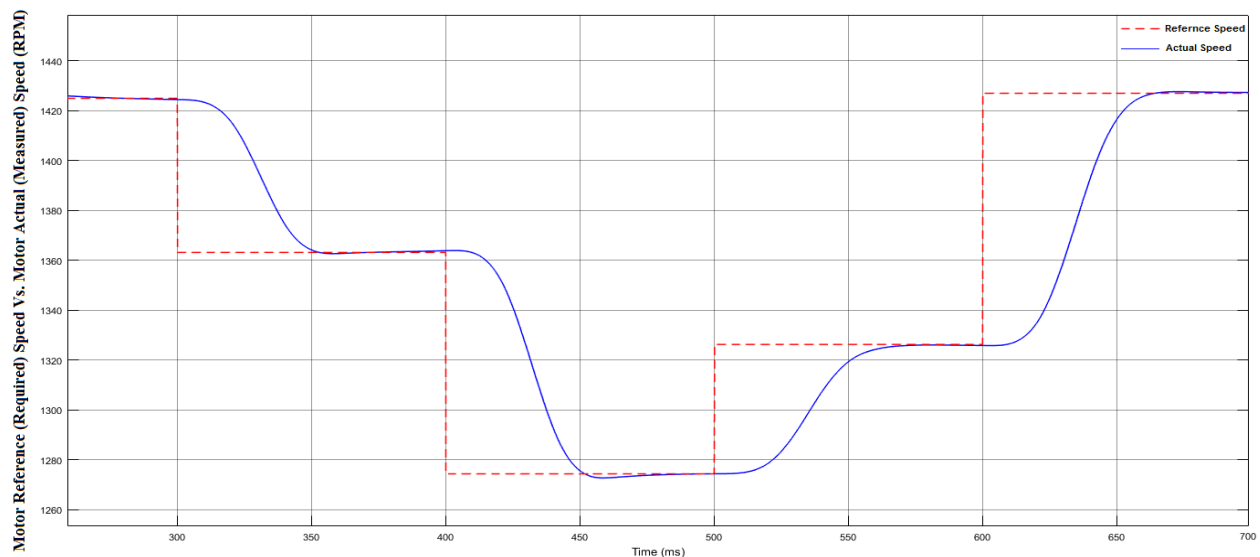


Figure-11. Motor reference speed vs. motor actual speed.

8. CONCLUSIONS

The IFOC speed control loop PI controller has been tuned using the particle swarm optimization (PSO) and the conventional Ziegler-Nichols (ZN) methods. The various results presented show that the proposed PSO method with different performance assessment indices has more robust stability and efficiency, and can solve the searching and tuning problems of PI controller gains more easily and quickly than the conventional ZN method.

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